

A One-Day Technology Transfer Event

The theory and practice of **PERFORMANCE-BASED DESIGN**

THE FUTURE OF EARTHQUAKE ENGINEERING

Instructor: Ashraf Habibullah
President and CEO, Computers & Structures, Inc.



NEW ANOTHER BREAKTHROUGH FROM RADIO SHACK!

TRS-80 MODEL II

5-Figure Computing Power at a 4-Figure Price!

Complete System from

3450⁰⁰

16 to 2 Million Bytes of Disk Storage
12 to 128 Keyboard Access Memory
Fast and Dependable

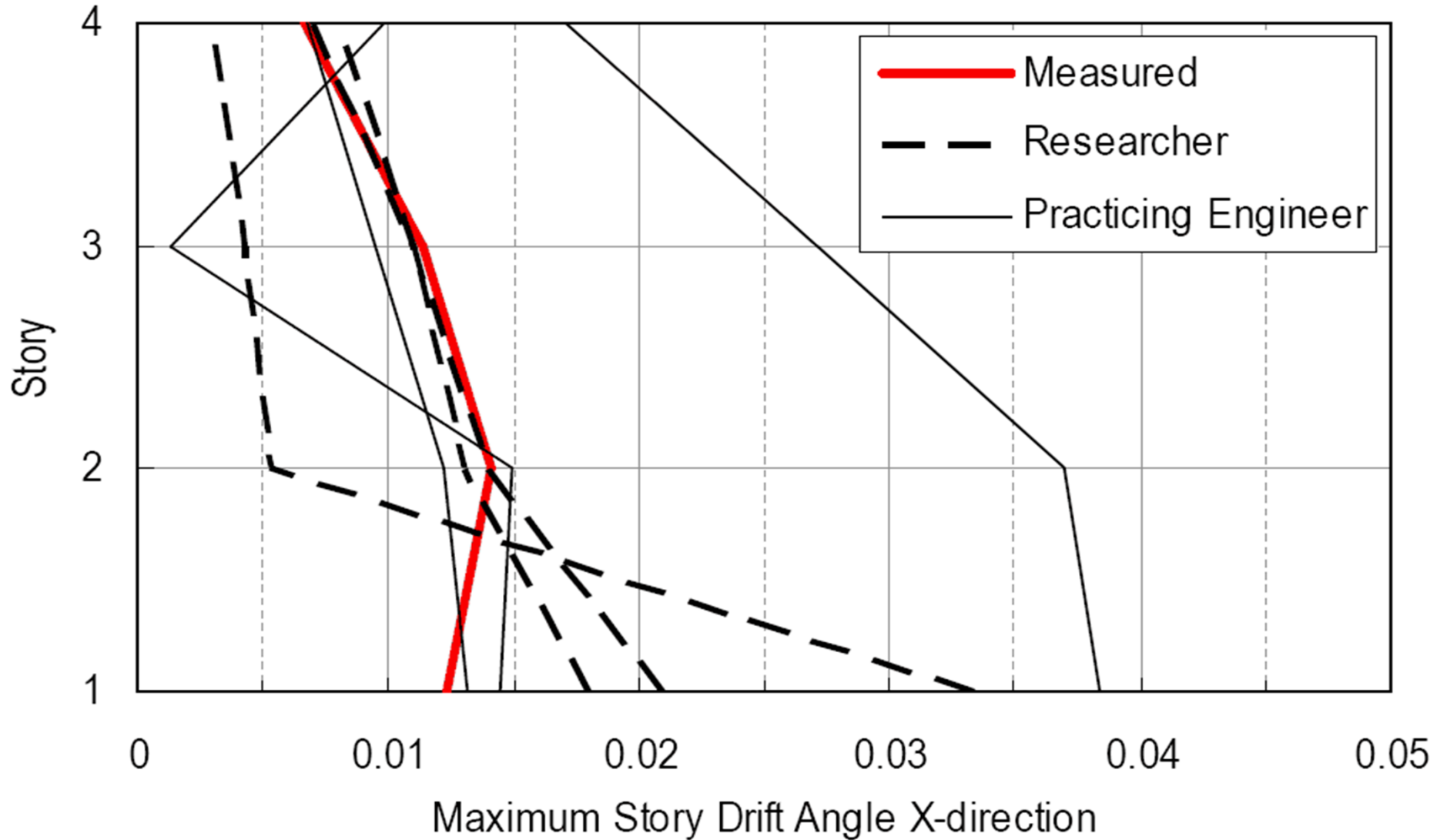
Supported at Any Radio Shack
Center With Over 5000 Sales
Locations and More Than 100
Service Centers

Radio Shack is engineering and manufacturing your TRS-80 Model II with 128K Bytes of 16-bit computer power. This is the original TRS-80 Model II computer system. It uses the same 16-bit TRS-80 Model II architecture as the 16-bit TRS-80 Model II computer system. It is the only 16-bit computer system that offers the same performance as the TRS-80 Model II computer system. And, it's the only 16-bit computer system that offers the same performance as the TRS-80 Model II computer system.



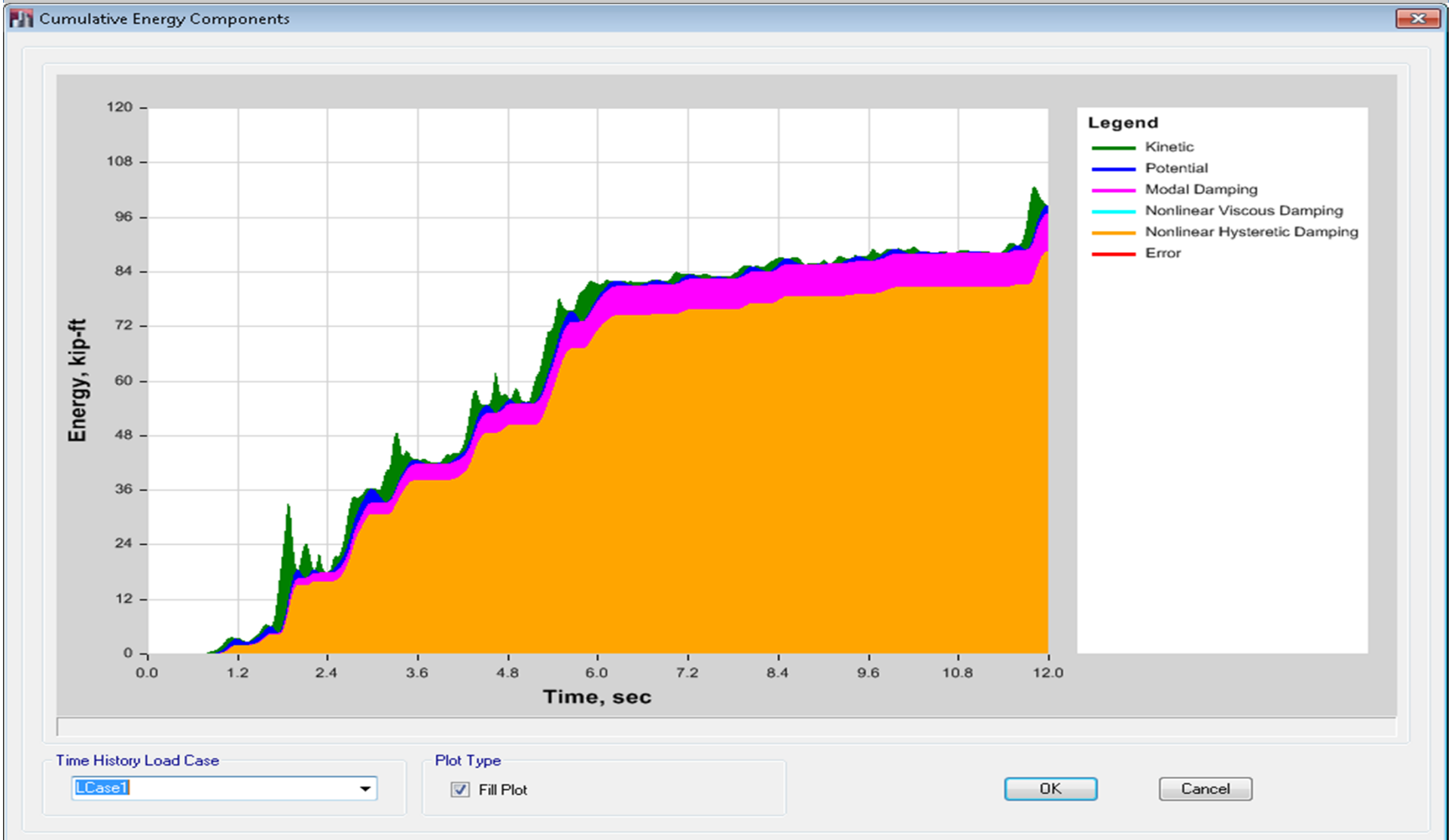


CALCULATED vs MEASURED





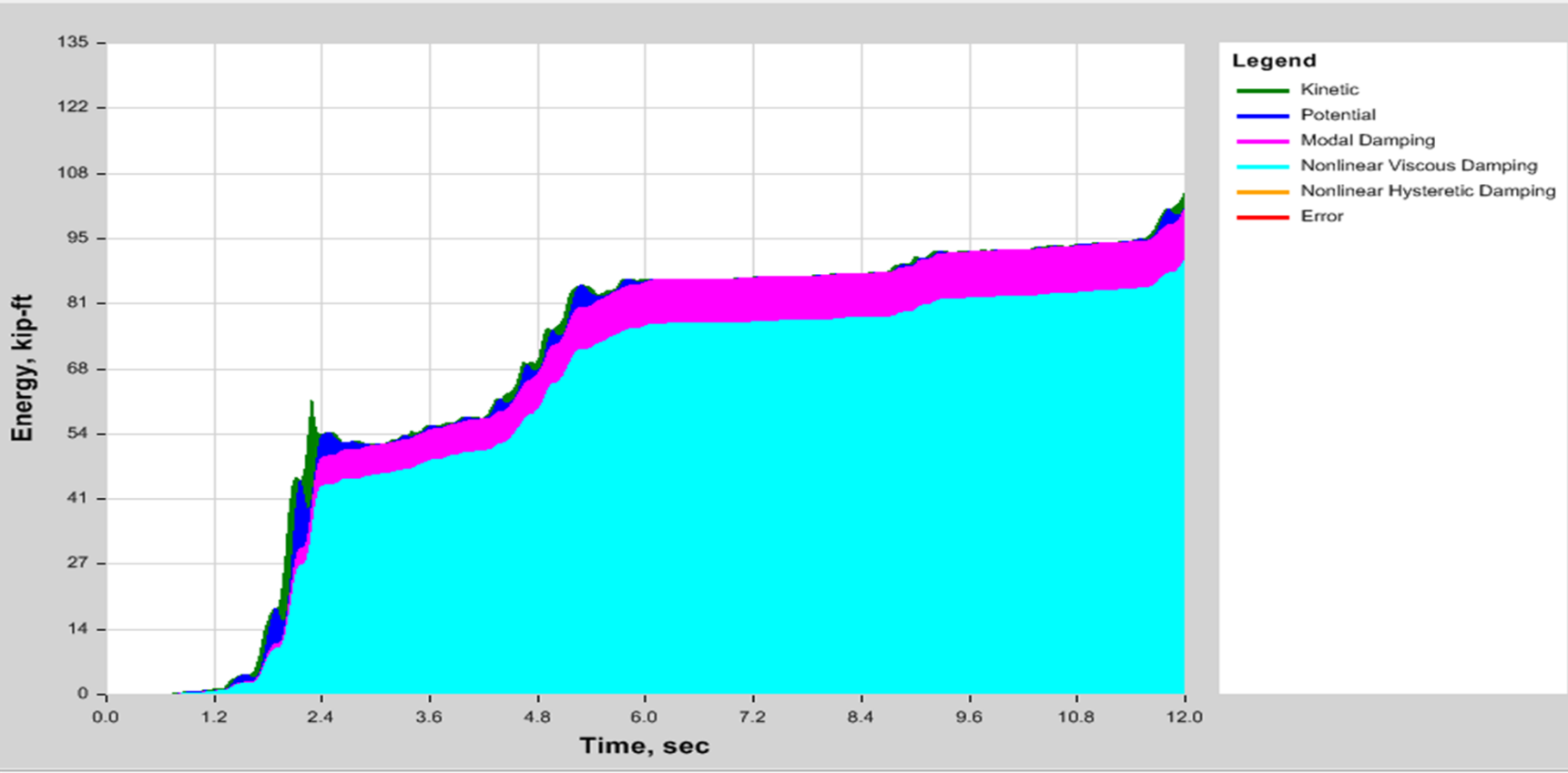
ENERGY DISSIPATION







Cumulative Energy Components



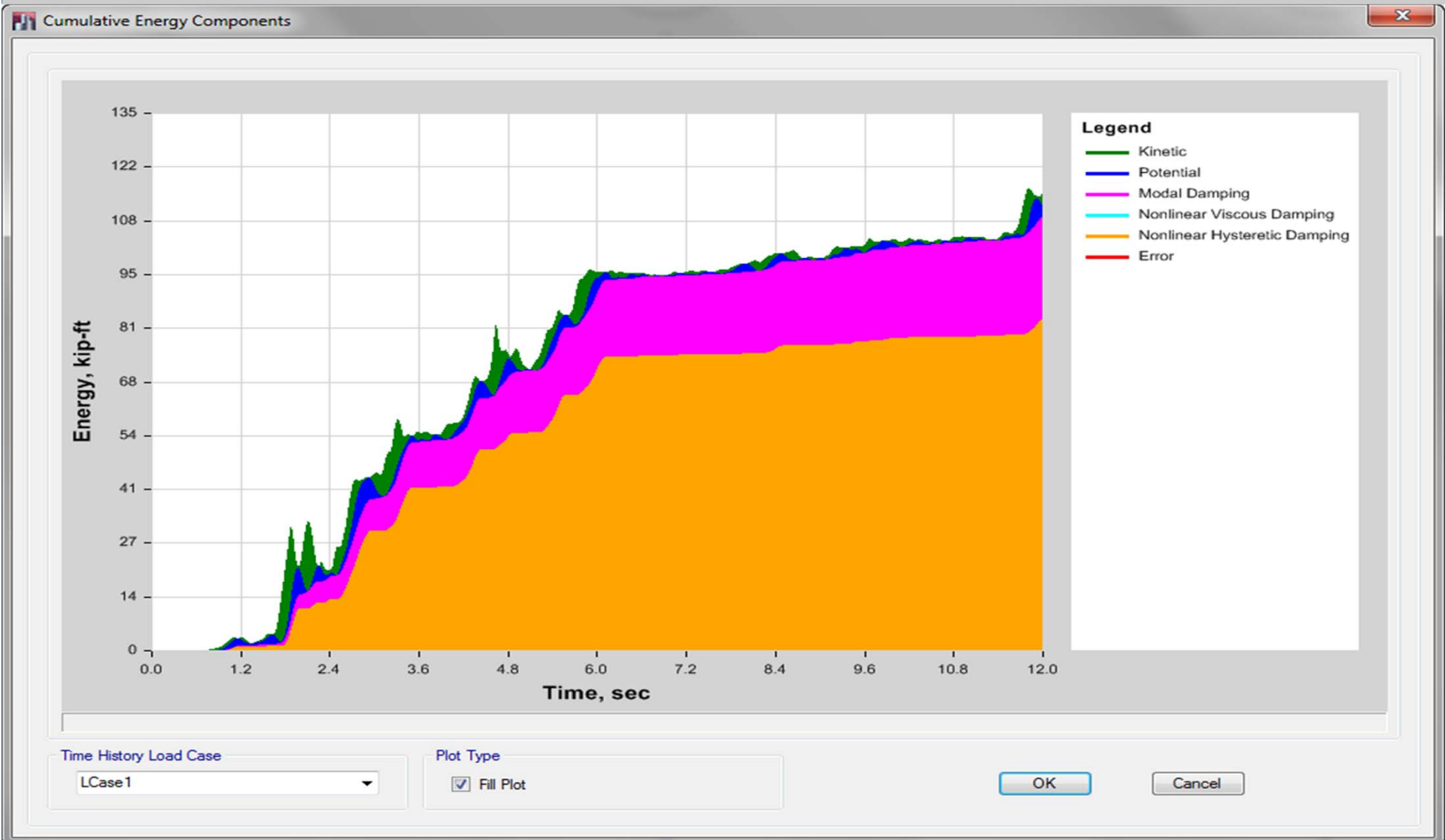
Time History Load Case
LCase1

Plot Type
 Fill Plot

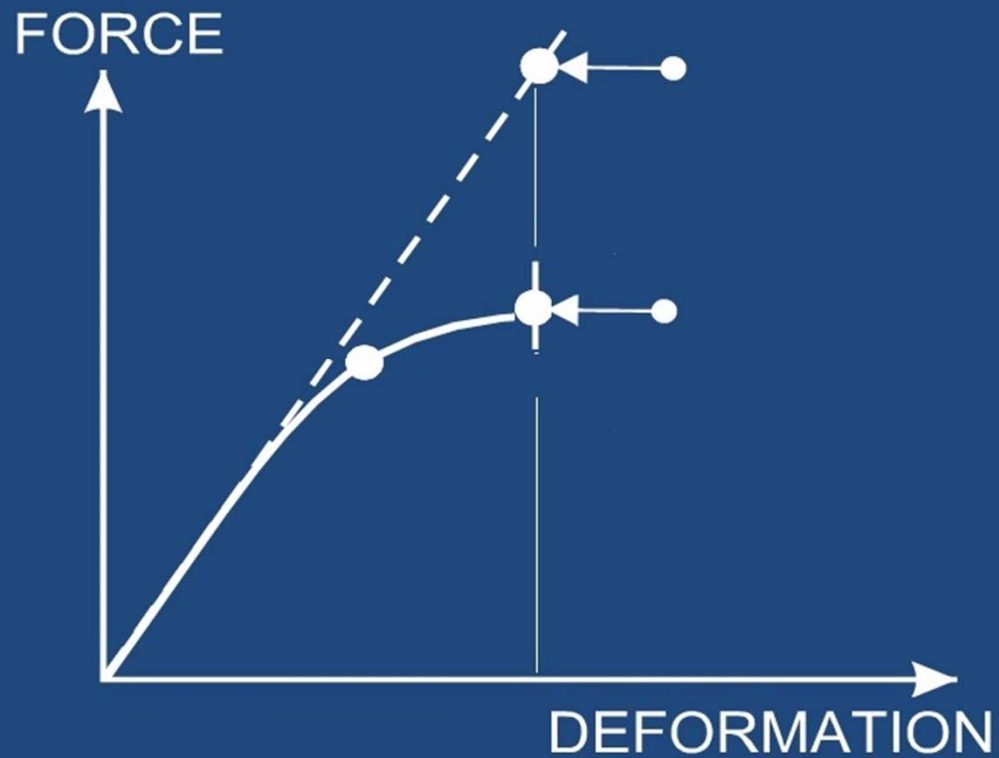
OK

Cancel



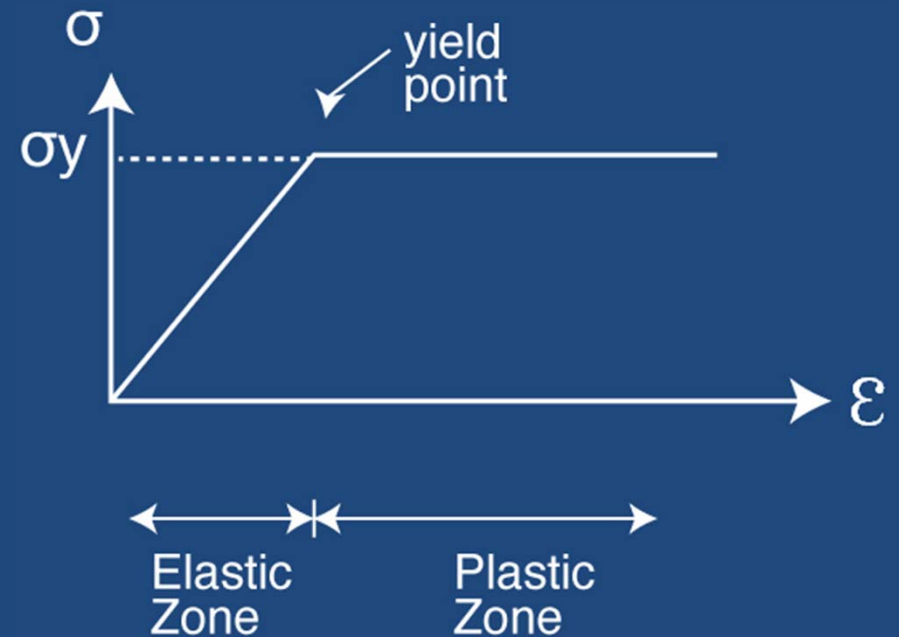
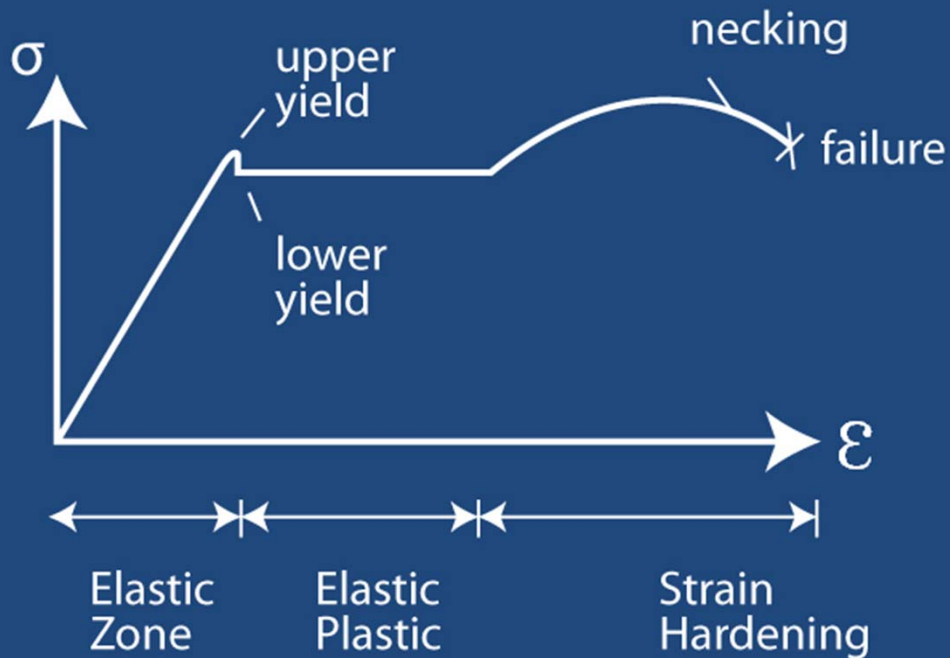


IMPLICIT NONLINEAR BEHAVIOR



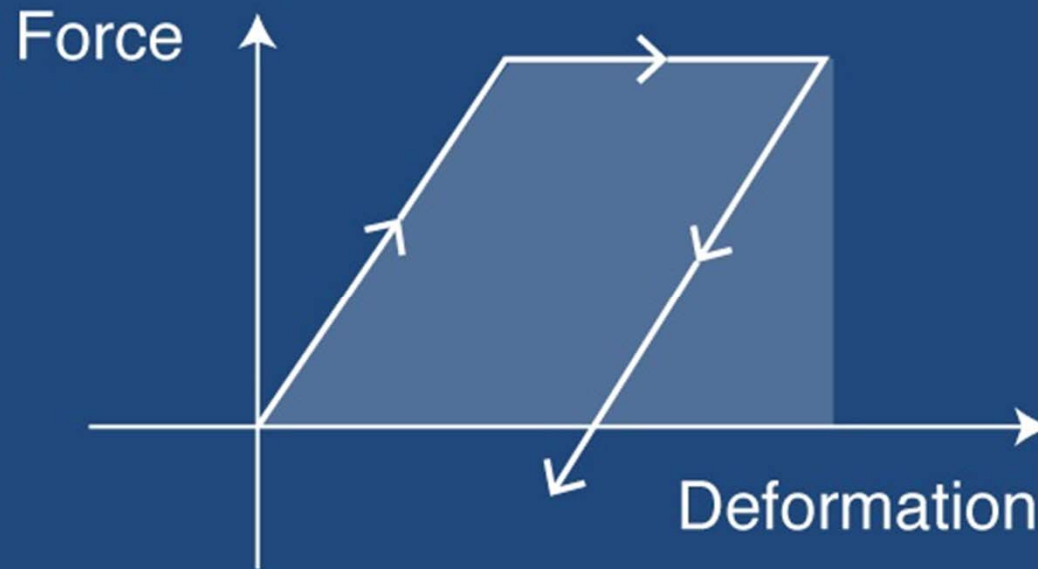


STEEL STRESS STRAIN RELATIONSHIPS



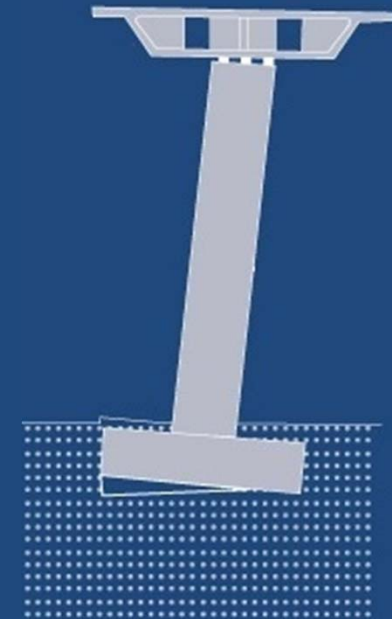


INELASTIC WORK DONE!

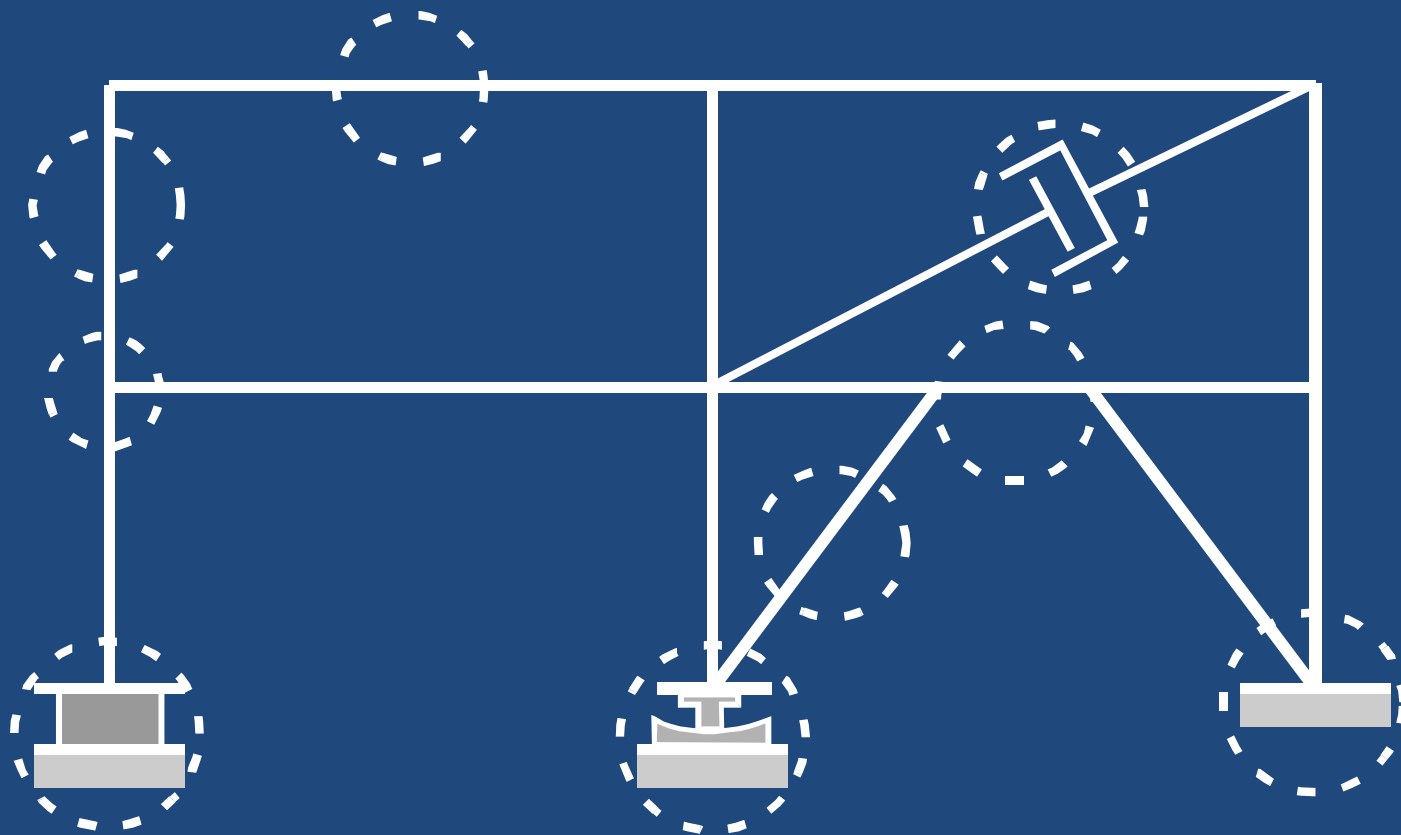


CAPACITY DESIGN

STRONG COLUMNS & WEAK BEAMS IN FRAMES
REDUCED BEAM SECTIONS
LINK BEAMS IN ECCENTRICALLY BRACED FRAMES
BUCKLING RESISTANT BRACES AS FUSES
RUBBER-LEAD BASE ISOLATORS
HINGED BRIDGE COLUMNS
HINGES AT THE BASE LEVEL OF SHEAR WALLS
ROCKING FOUNDATIONS
OVERDESIGNED COUPLING BEAMS
OTHER SACRIFICIAL ELEMENTS



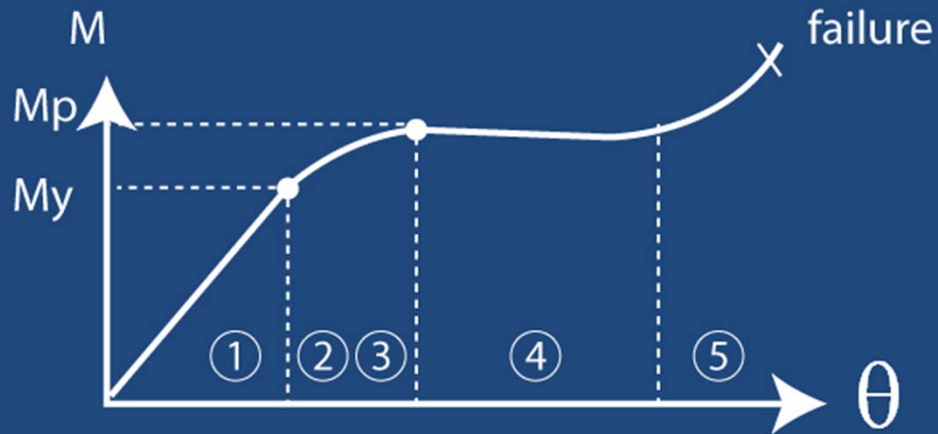
STRUCTURAL COMPONENTS



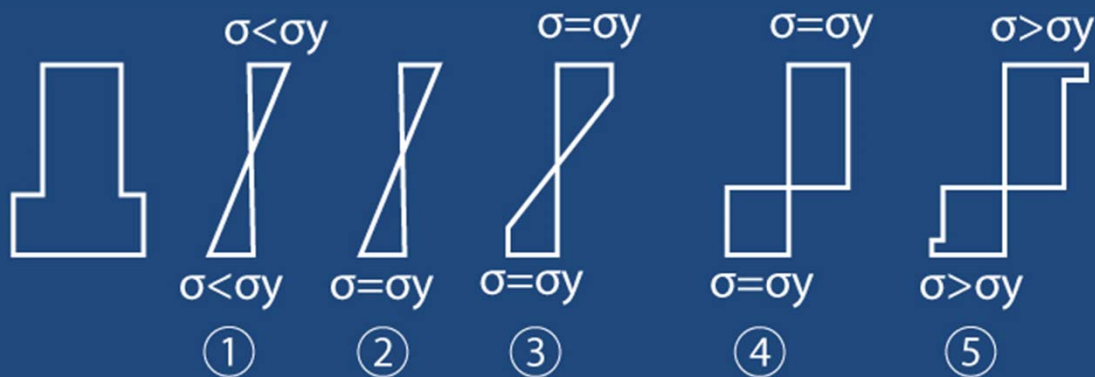
Nonlinear Analysis & Performance Based Design



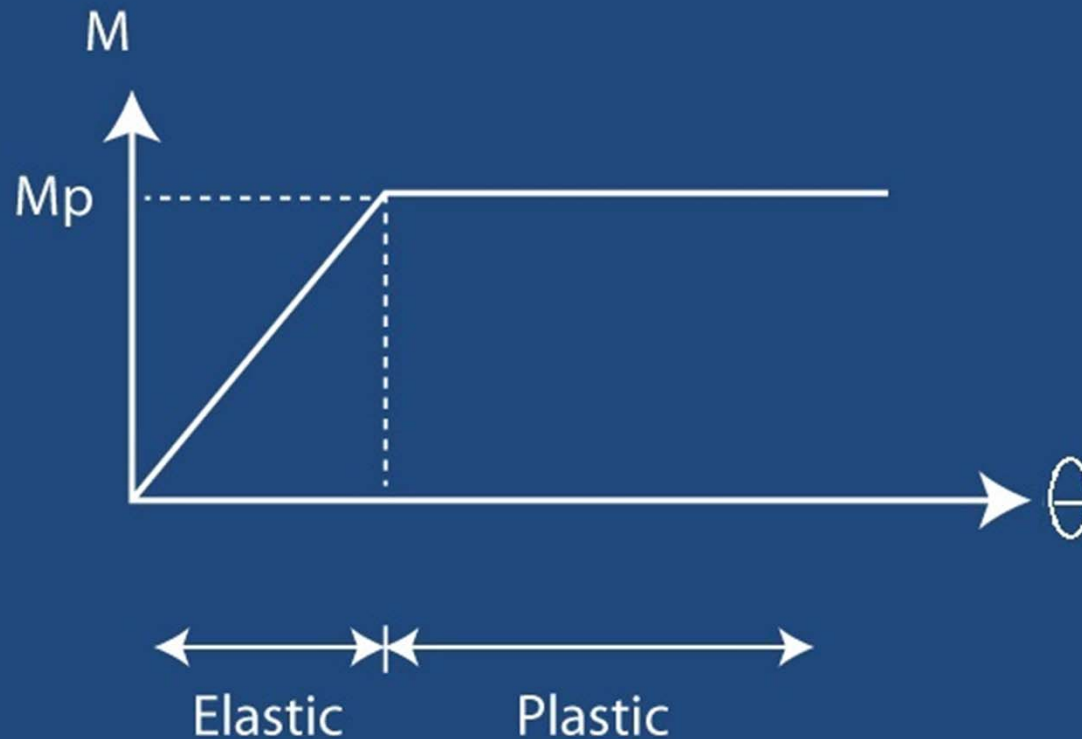
MOMENT ROTATION RELATIONSHIP



\leftarrow Elastic \leftarrow Elastic Plastic \leftarrow Plastic \leftarrow Strain Hardening \rightarrow



IDEALIZED MOMENT ROTATION





PERFORMANCE LEVELS

Expected Post-Earthquake Damage State

Operational

Backup utility services maintain functions; very little damage.

Immediate Occupancy

The building remains safe to occupy; any repairs are minor.

Life Safety

Structure remains stable and has significant reserve capacity; hazardous nonstructural damage is controlled.

Collapse Prevention

The building remains standing, but only barely; any other damage or loss is acceptable.

Higher Performance

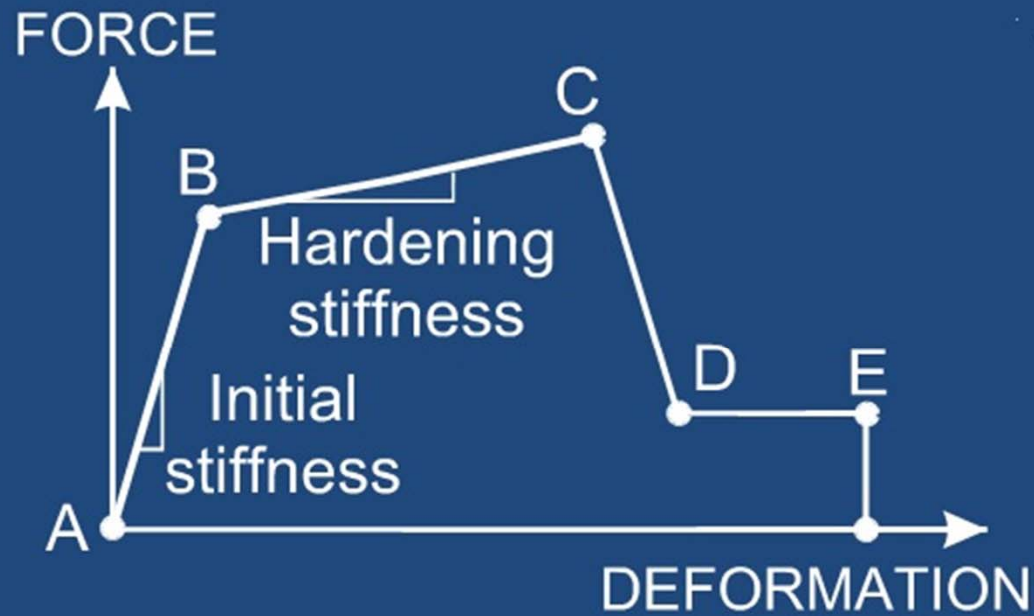
less loss



Lower Performance

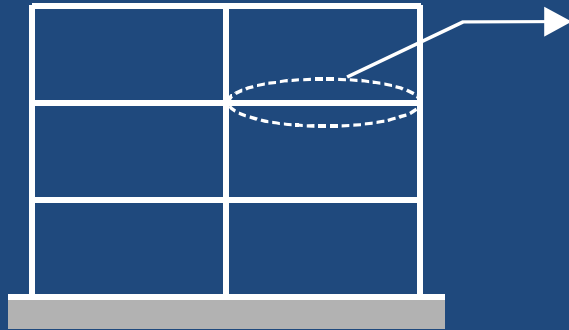
more loss

IDEALIZED FORCE DEFORMATION CURVE

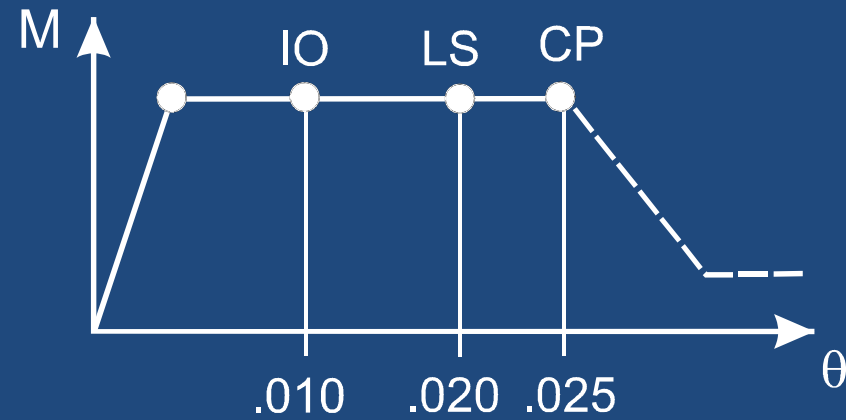
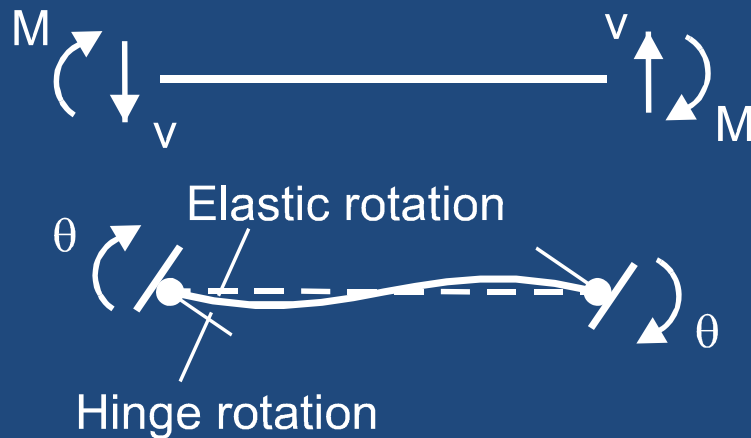


ASCE 41

ASCE 41 BEAM MODEL



Performance assessment :
Bending behavior is ductile.
Use hinge rotation D/C ratio.



ASCE 41 hinge rotation capacities

ASCE 41 ASSESSMENT OPTIONS

- Linear Static Analysis
- Linear Dynamic Analysis
(Response Spectrum or Time History Analysis)
- Nonlinear Static Analysis
(Pushover Analysis)
- Nonlinear Dynamic Time History Analysis
(NDI or FNA)

STRENGTH vs DEFORMATION

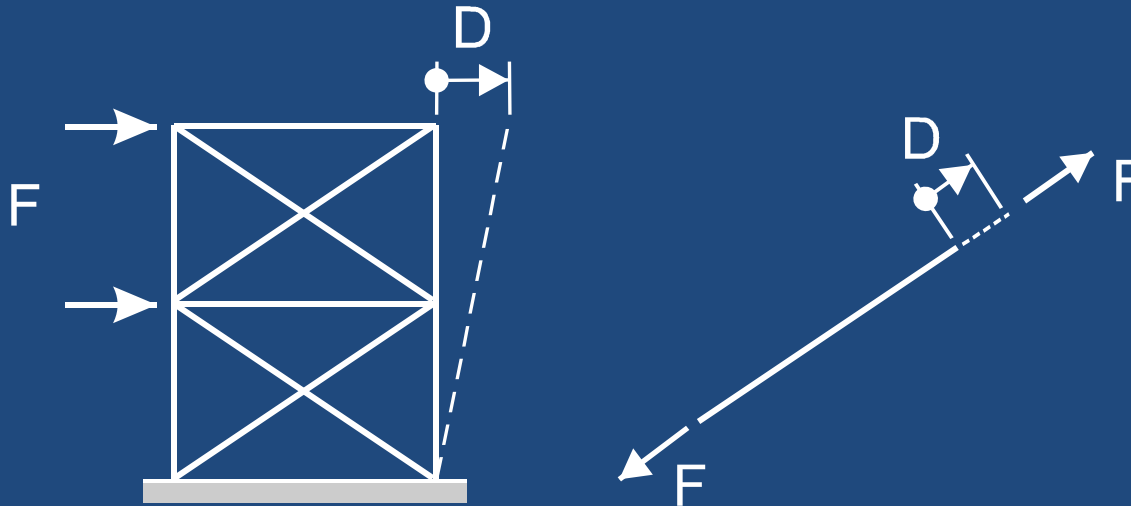
ELASTIC STRENGTH DESIGN - KEY STEPS

CHOOSE DESIGN CODE AND EARTHQUAKE LOADS
DESIGN CHECK PARAMETERS STRESS/BEAM MOMENT
GET ALLOWABLE STRESSES/ULTIMATE – PHI FACTORS
CALCULATE STRESSES – LOAD FACTORS (STRESS)
CALCULATE STRESS RATIOS

INELASTIC DEFORMATION BASED DESIGN -- KEY STEPS

CHOOSE PERFORMANCE LEVEL AND DESIGN LOADS – ASCE 41
DEMAND CAPACITY MEASURES – DRIFT/HINGE ROTATION/SHEAR
GET DEFORMATION AND FORCE CAPACITIES
CALCULATE DEFORMATION AND FORCE DEMANDS (STRESS)
CALCULATE D/C RATIOS – LIMIT STATES

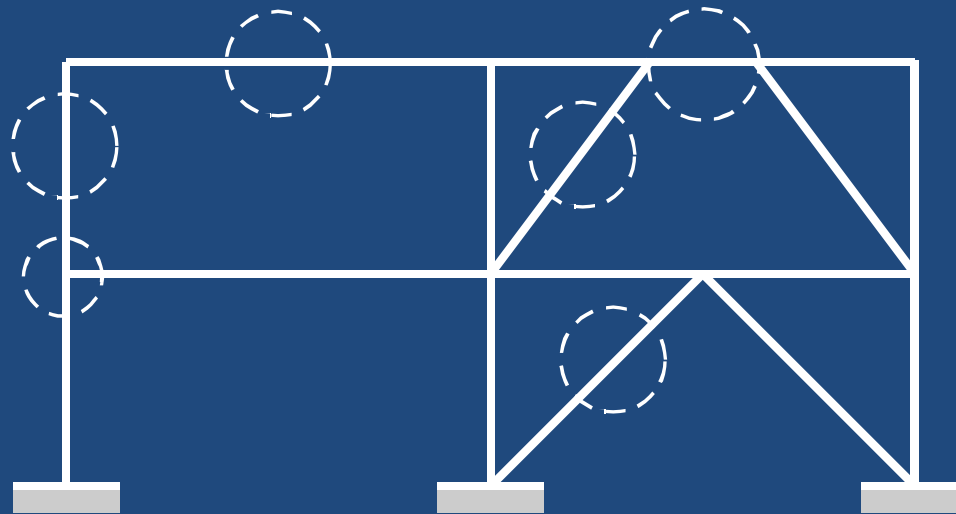
STRUCTURE and MEMBERS



- For a structure, $F = \text{load}$, $D = \text{deflection}$.
- For a component, F depends on the component type, D is the corresponding deformation.
- The component F - D relationships must be known.
- The structure F - D relationship is obtained by structural analysis.



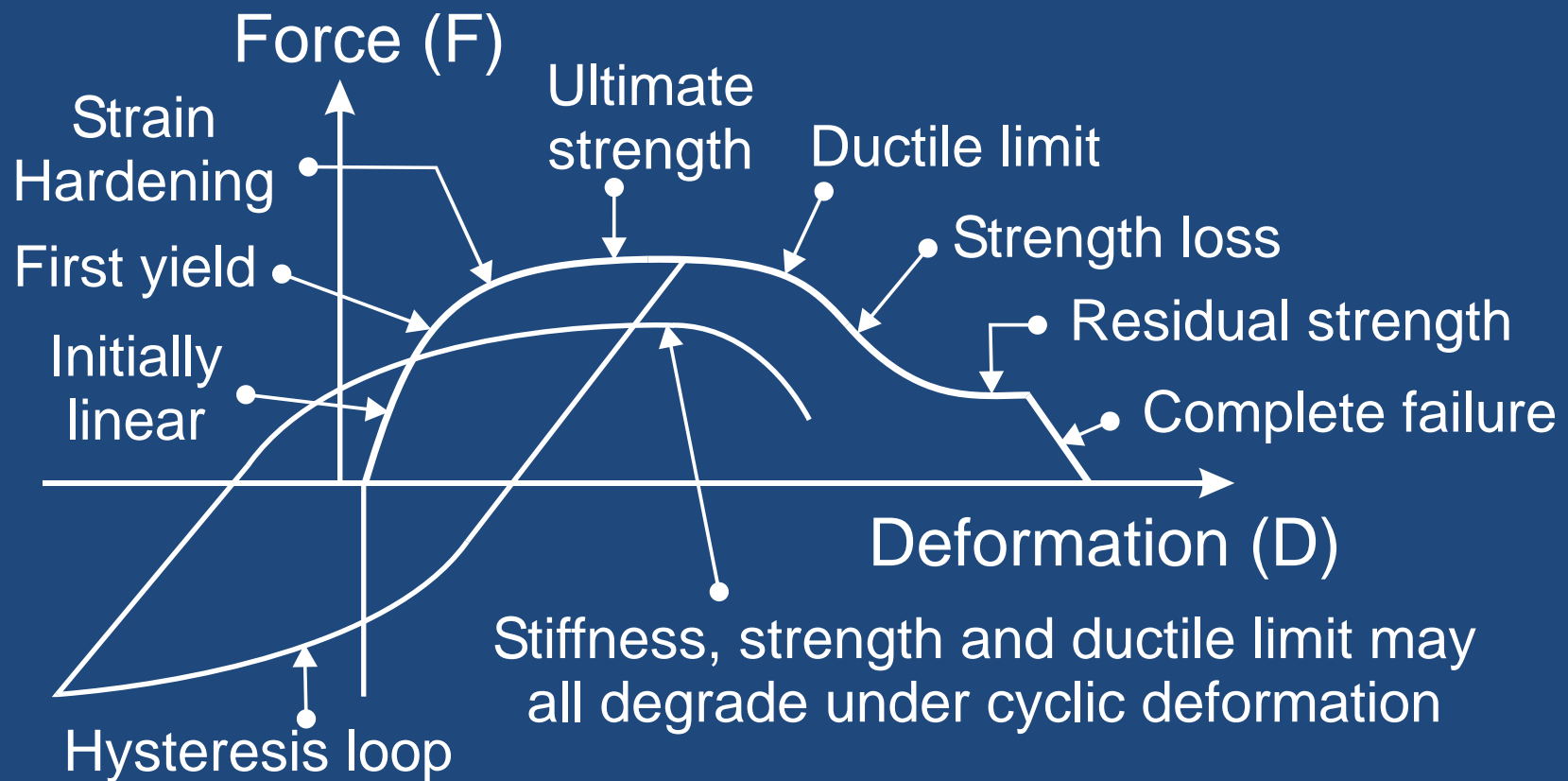
FRAME COMPONENTS



- For each component type we need :
 - Reasonably accurate nonlinear F-D relationships.
 - Reasonable deformation and/or strength capacities.
- We must choose realistic demand-capacity measures, and it must be feasible to calculate the demand values.
- The best model is the simplest model that will do the job.

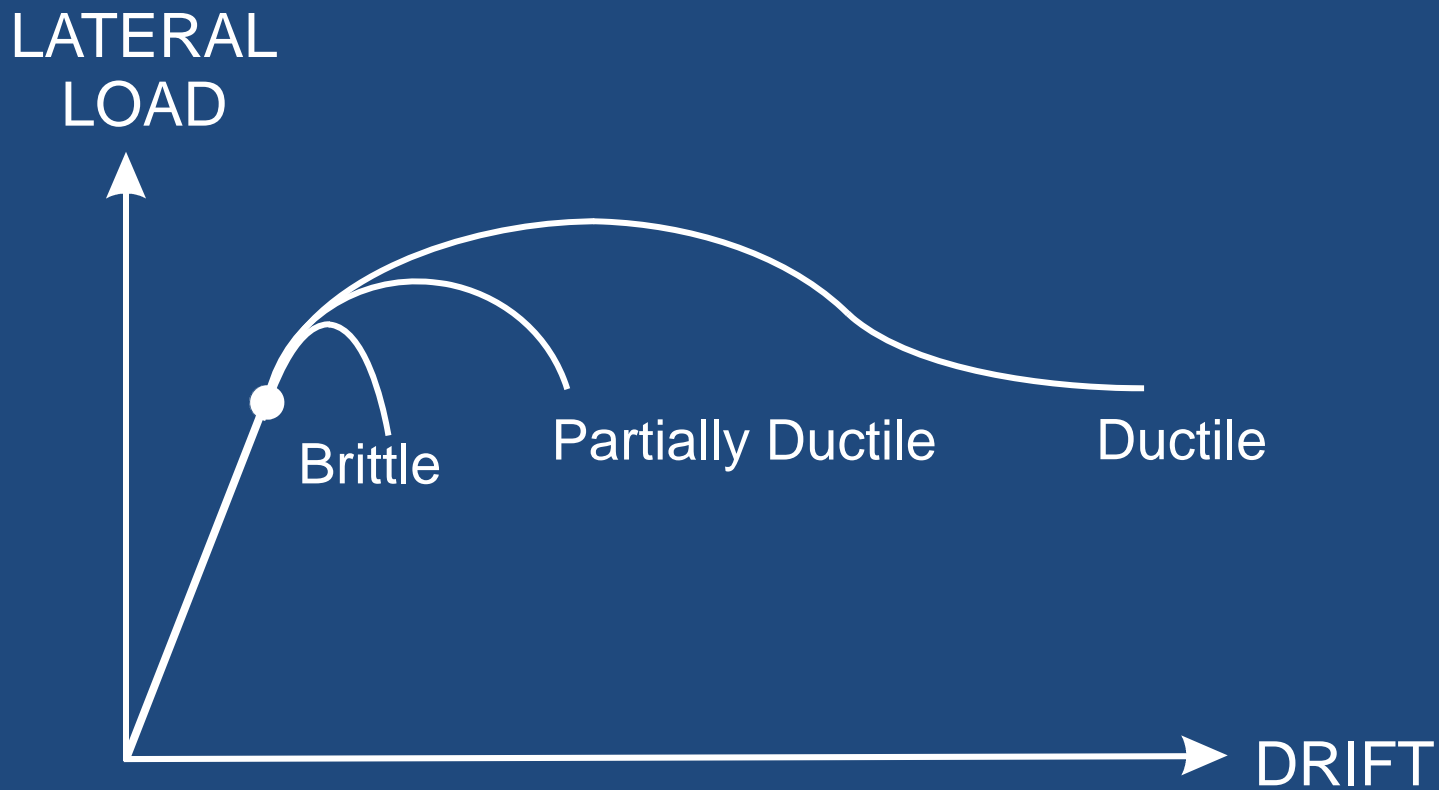


F-D RELATIONSHIP

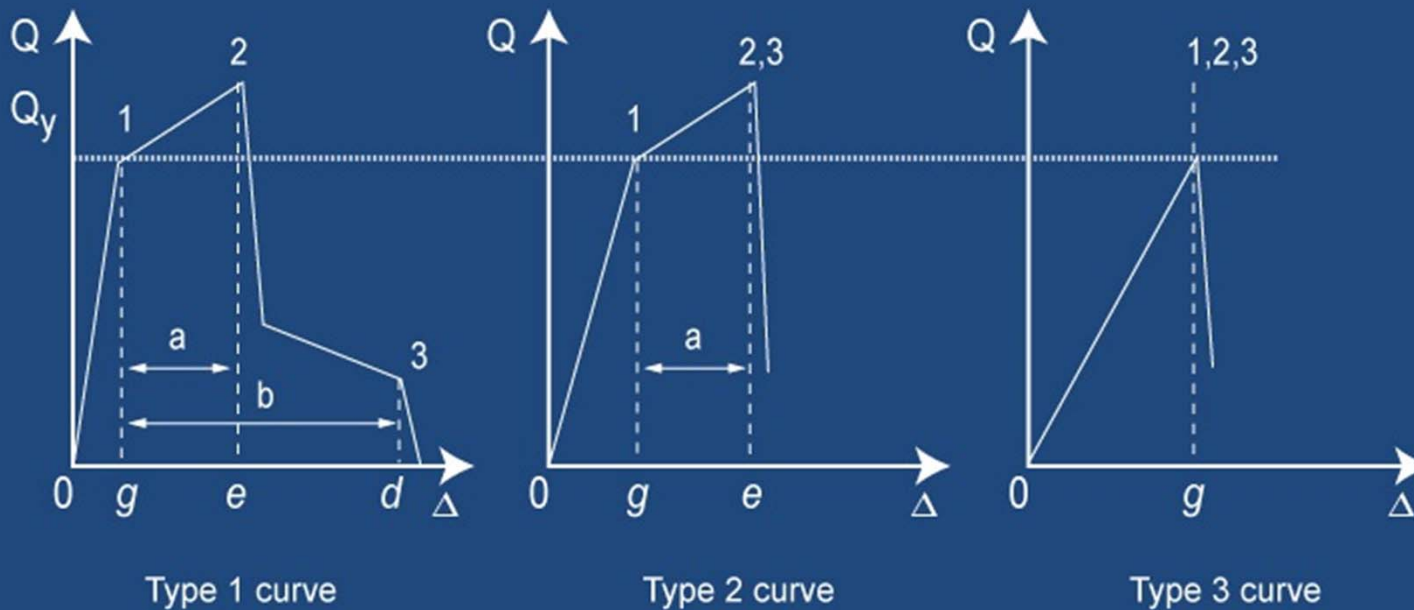




DUCTILITY



ASCE 41 - DUCTILE AND BRITTLE

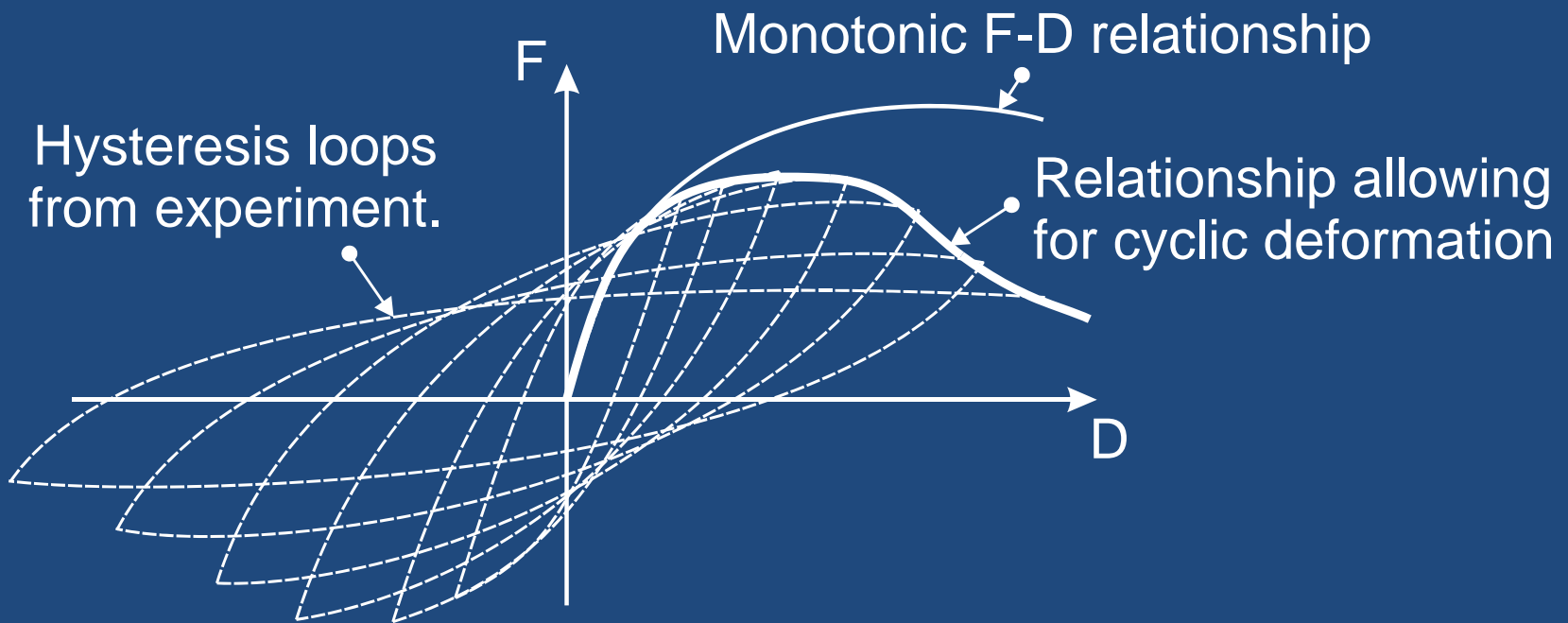


FORCE AND DEFORMATION CONTROL

Component	Deformation-Controlled Action	Force-Controlled Action
Moment Frames <ul style="list-style-type: none"> • Beams • Columns • Joints 	Moment (M) M --	Shear (V) Axial load (P), V V
Shear Walls	M, V	P
Braced Frames <ul style="list-style-type: none"> • Braces • Beams • Columns • Shear Link 	P -- -- V	-- P P P, M
Connections	P, V, M	P, V, M
Diaphragms	M, V	P, V, M

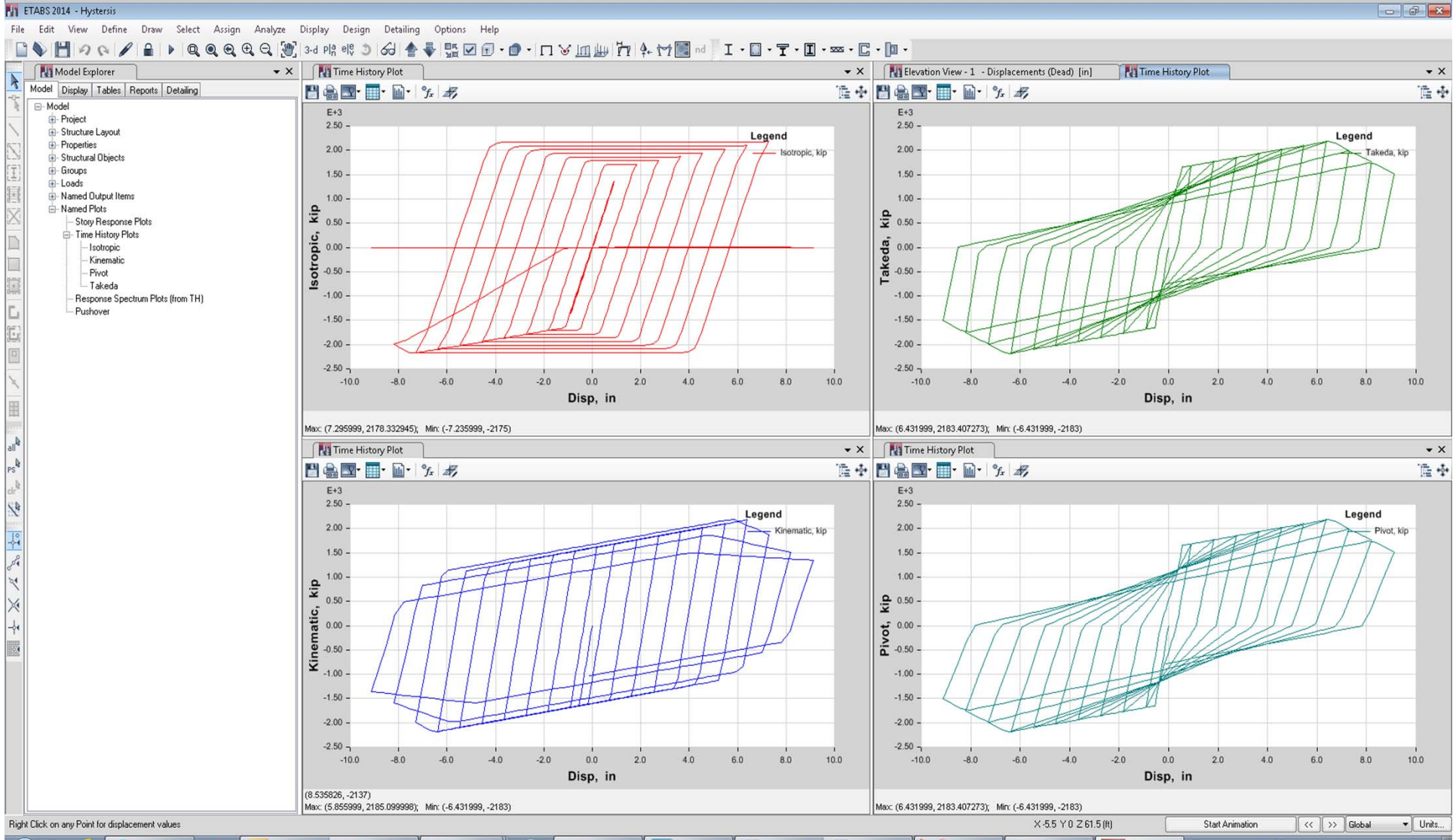


BACKBONE CURVE





HYSTERESIS LOOP MODELS

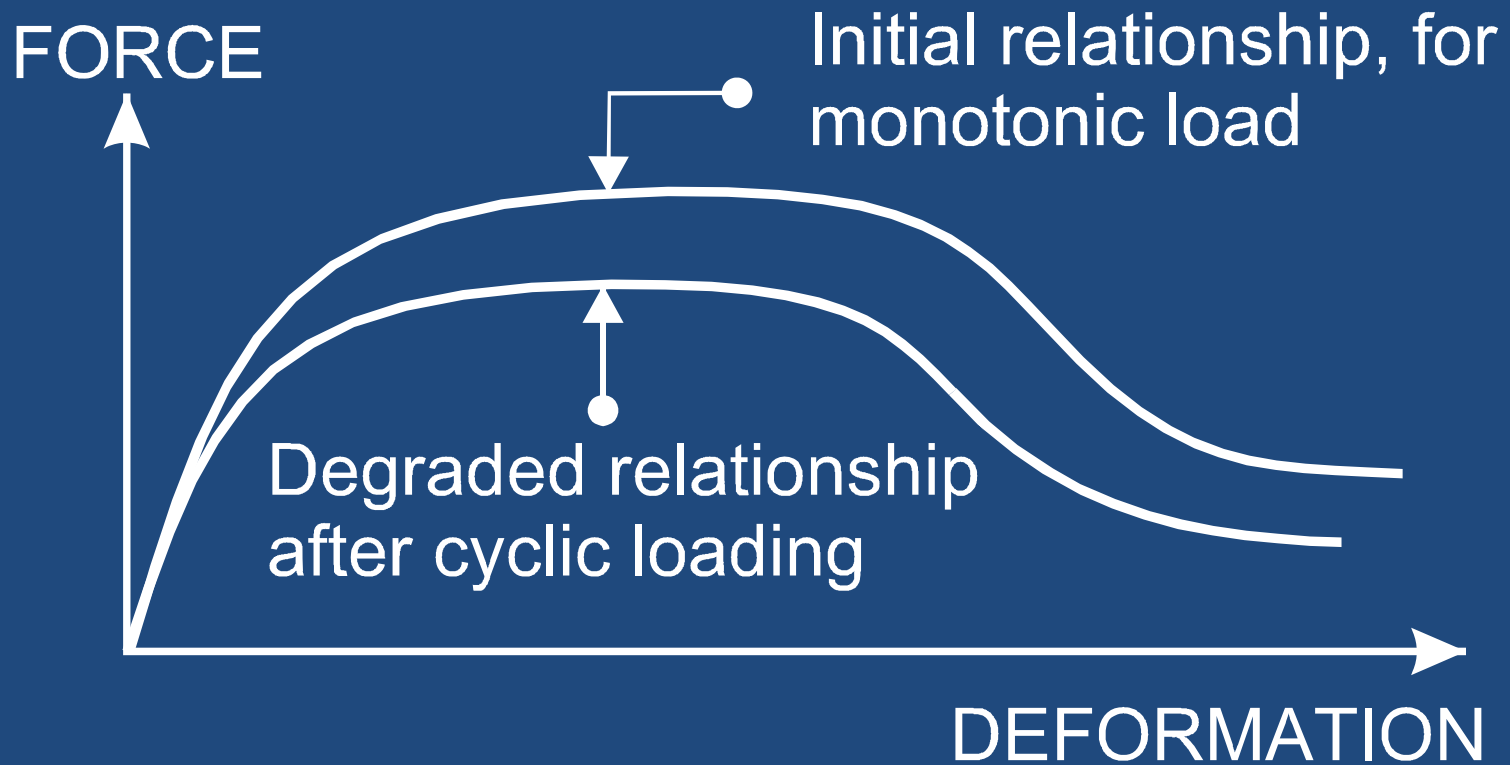


Nonlinear Analysis & Performance Based Design

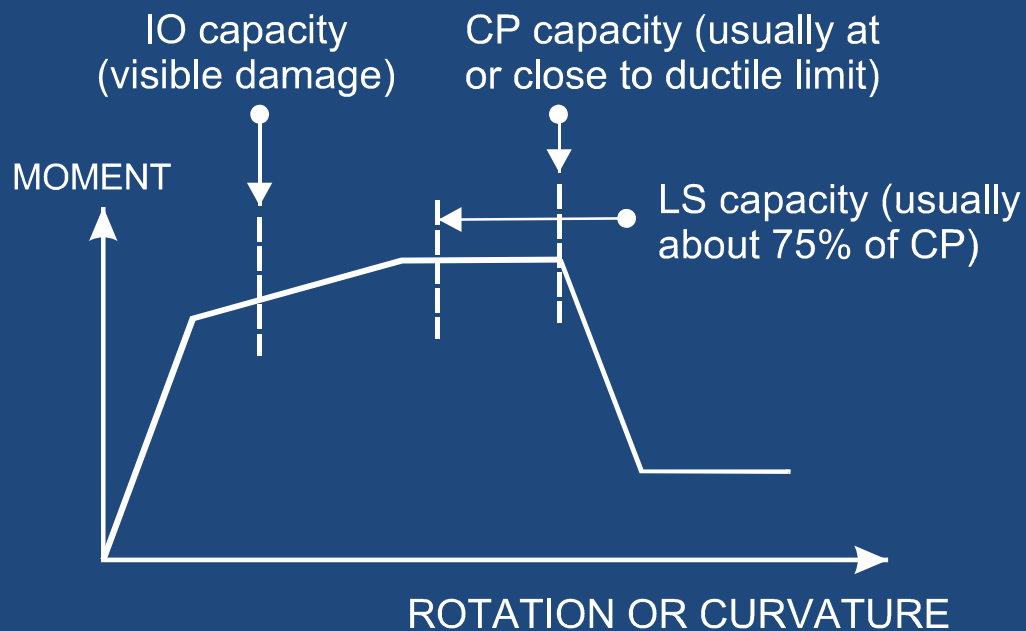




STRENGTH DEGRADATION



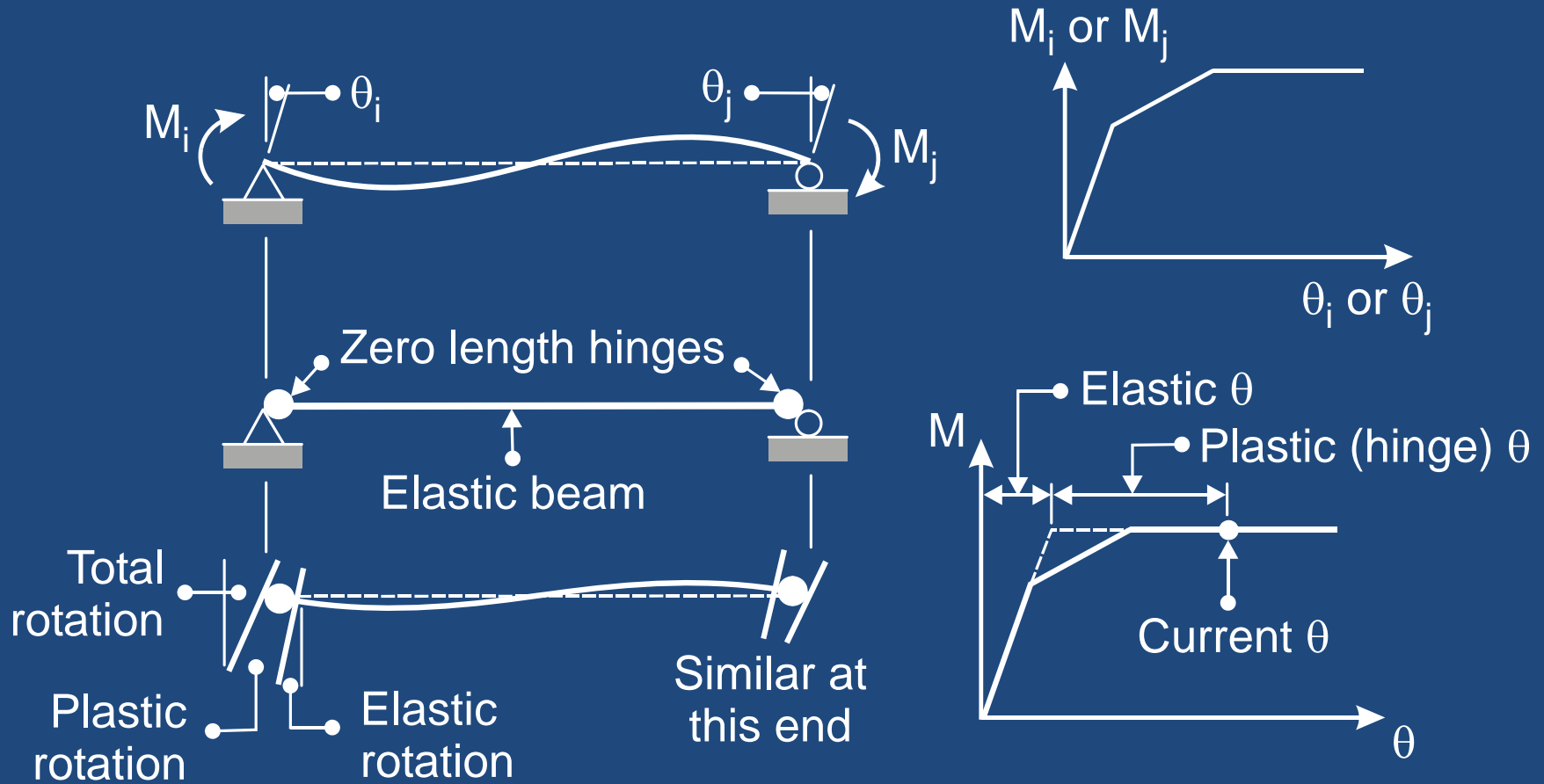
ASCE 41 DEFORMATION CAPACITIES



- This can be used for components of all types.
- It can be used if experimental results are available.
- ASCE 41 gives capacities for many different components.
- For beams and columns, ASCE 41 gives capacities only for the chord rotation model.

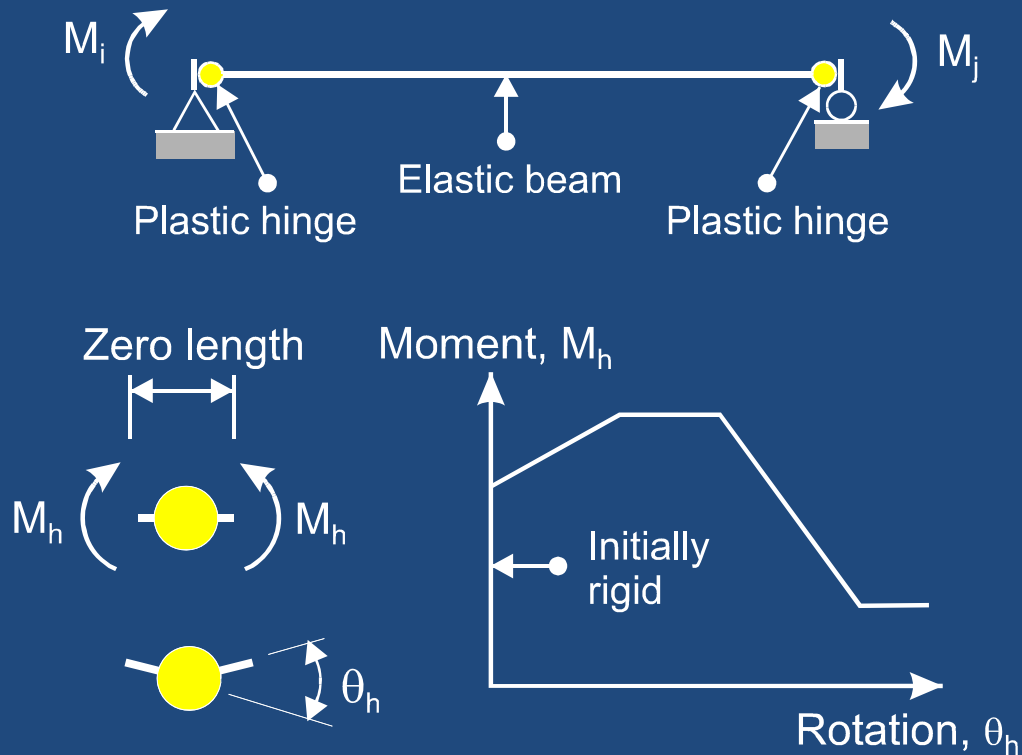


BEAM END ROTATION MODEL



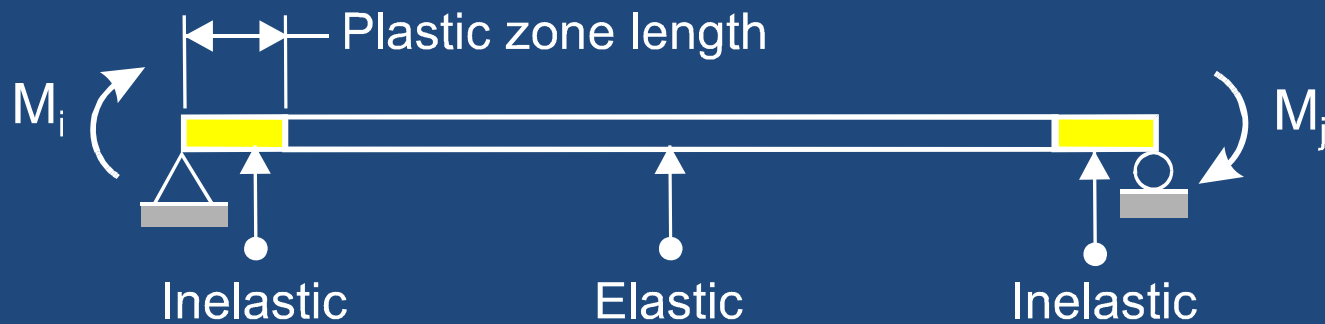


PLASTIC HINGE MODEL



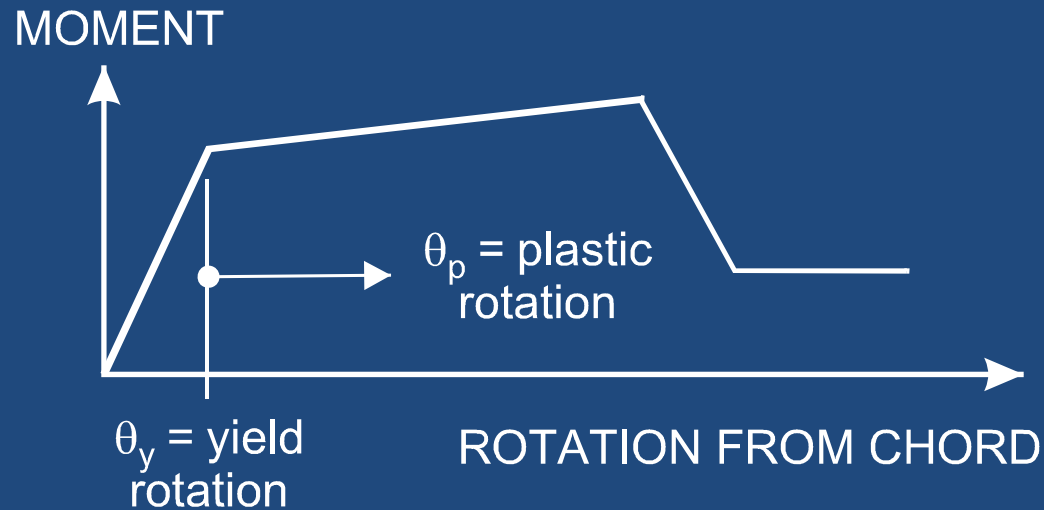
- It is assumed that all inelastic deformation is concentrated in zero-length plastic hinges.
- The deformation measure for D/C is hinge rotation.

PLASTIC ZONE MODEL



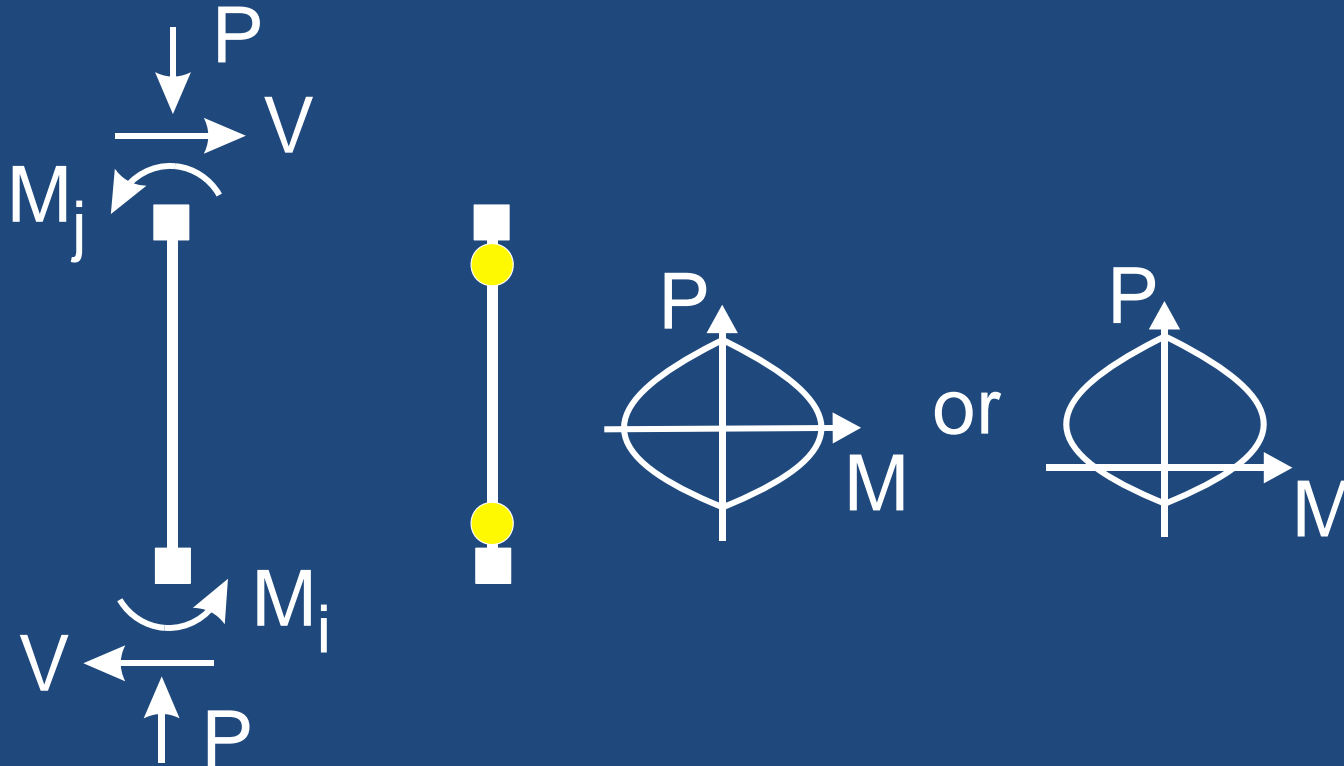
- The inelastic behavior occurs in finite length plastic zones.
- Actual plastic zones usually change length, but models that have variable lengths are too complex.
- The deformation measure for D/C can be :
 - Average curvature in plastic zone.
 - Rotation over plastic zone (= average curvature x plastic zone length).

ASCE 41 CHORD ROTATION CAPACITIES

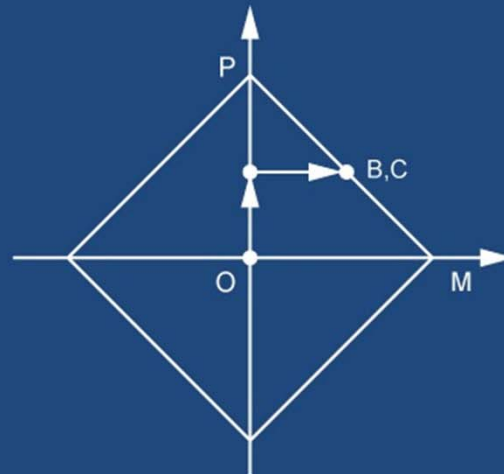
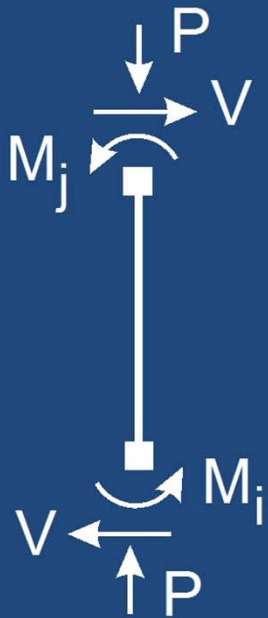


	IO	LS	CP
Steel Beam	$\theta_p / \theta_y = 1$	$\theta_p / \theta_y = 6$	$\theta_p / \theta_y = 8$
RC Beam			
Low shear	$\theta_p = 0.01$	$\theta_p = 0.02$	$\theta_p = 0.025$
High shear	$\theta_p = 0.005$	$\theta_p = 0.01$	$\theta_p = 0.02$

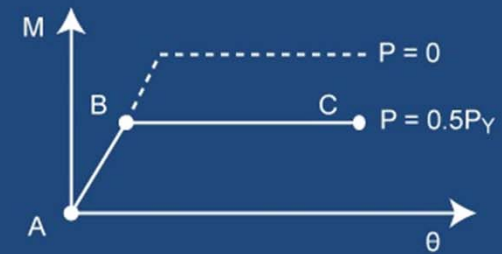
COLUMN AXIAL-BENDING MODEL



STEEL COLUMN AXIAL-BENDING



LOAD PATH

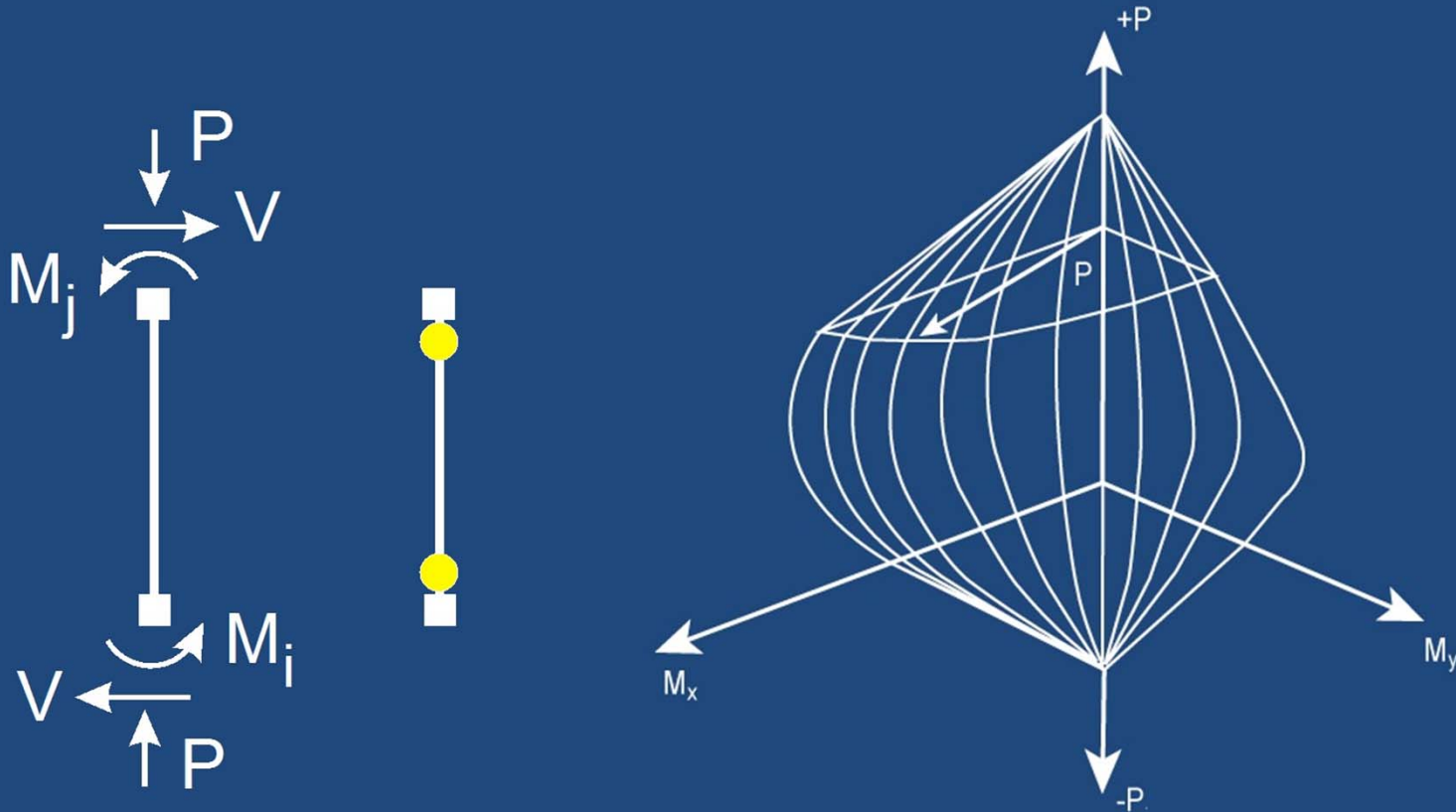


MOMENT ROTATION

$$M_y = Z F_y (1 - P / P_y)$$

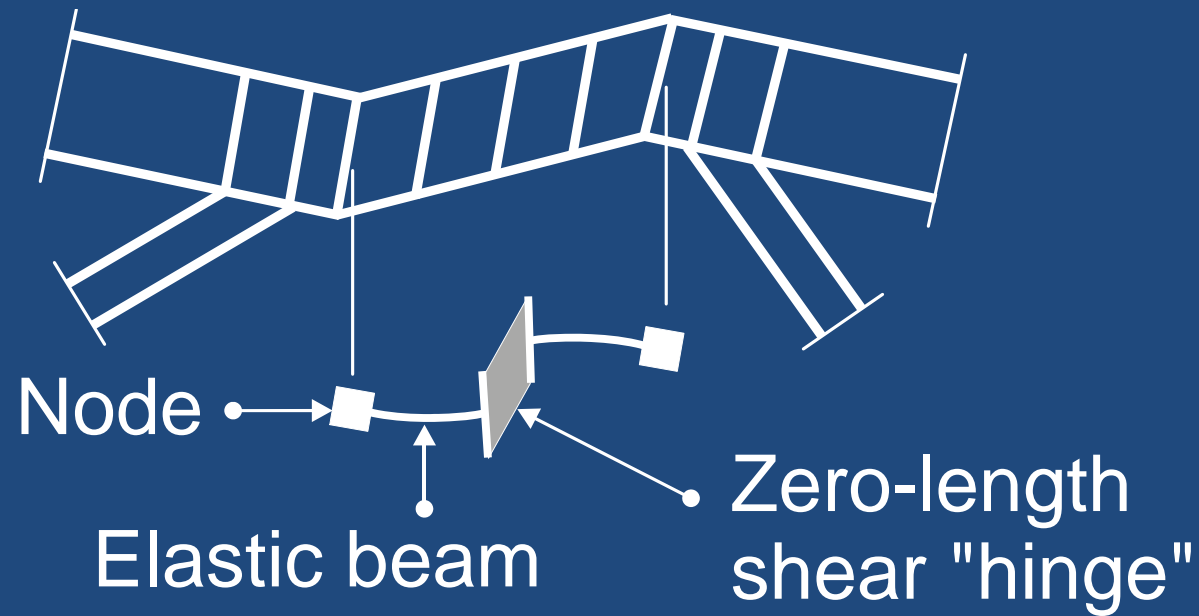


CONCRETE COLUMN AXIAL-BENDING



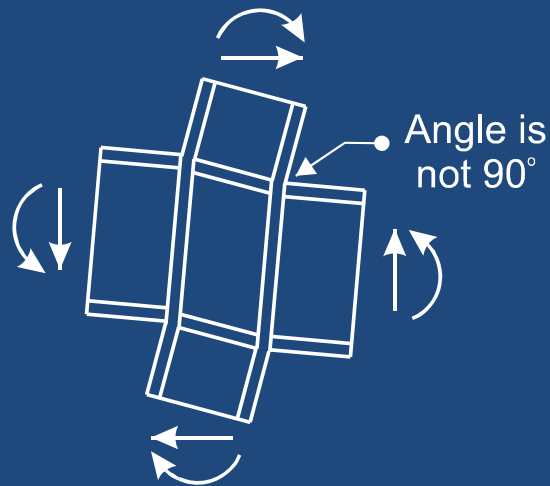


SHEAR HINGE MODEL

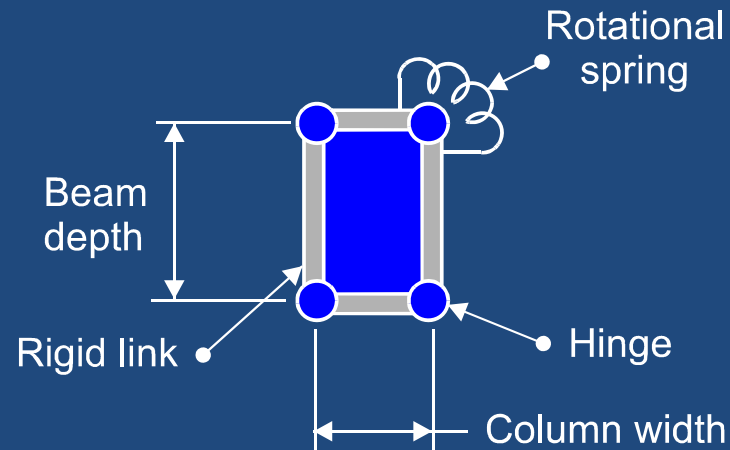




PANEL ZONE ELEMENT



PANEL ZONE DEFORMATION

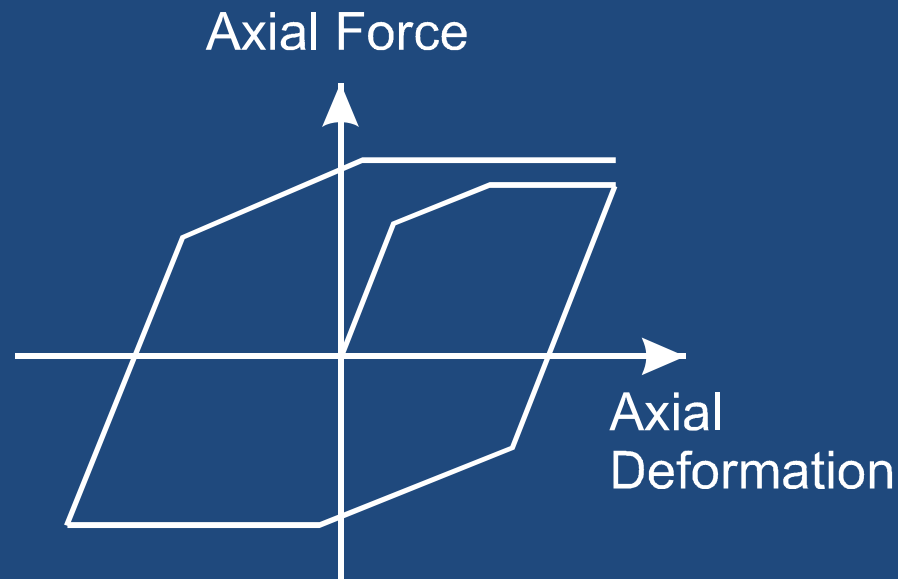


ANALYSIS MODEL

- Deformation, D = spring rotation = shear strain in panel zone.
- Force, F = moment in spring = moment transferred from beam to column elements.
- Also, $F = (\text{panel zone horizontal shear force}) \times (\text{beam depth})$.

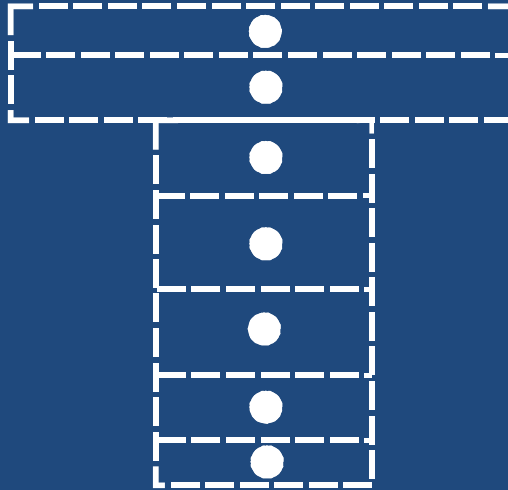


BUCKLING-RESTRAINED BRACE



The BRB element includes “isotropic” hardening.
The D-C measure is axial deformation.

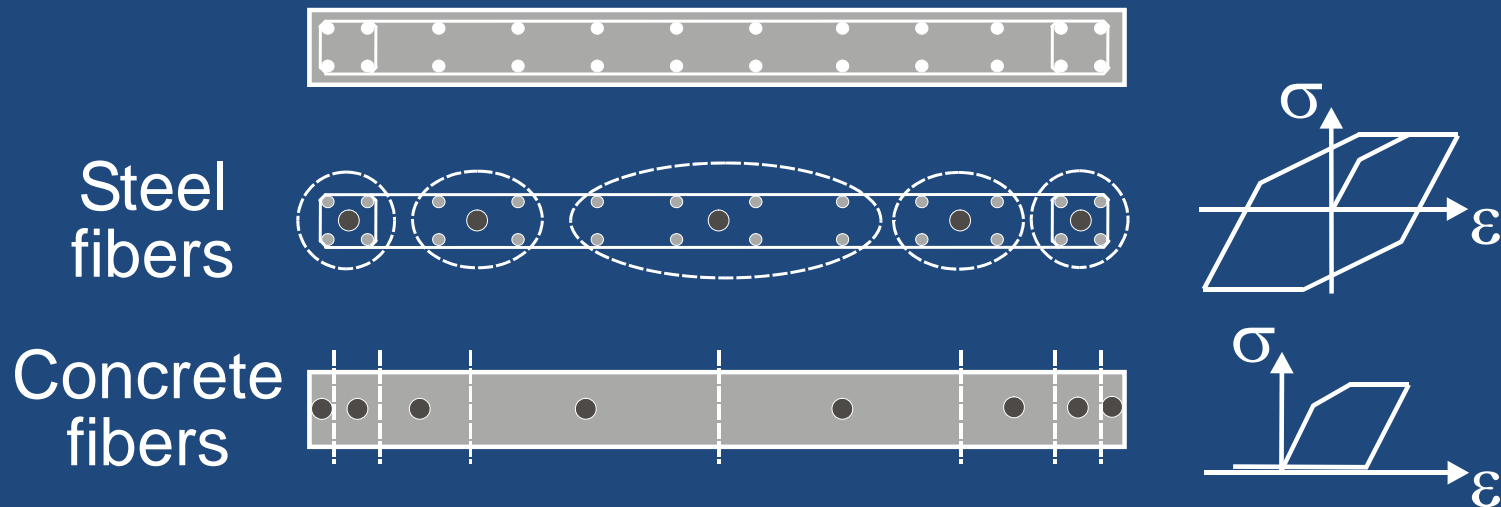
BEAM/COLUMN FIBER MODEL



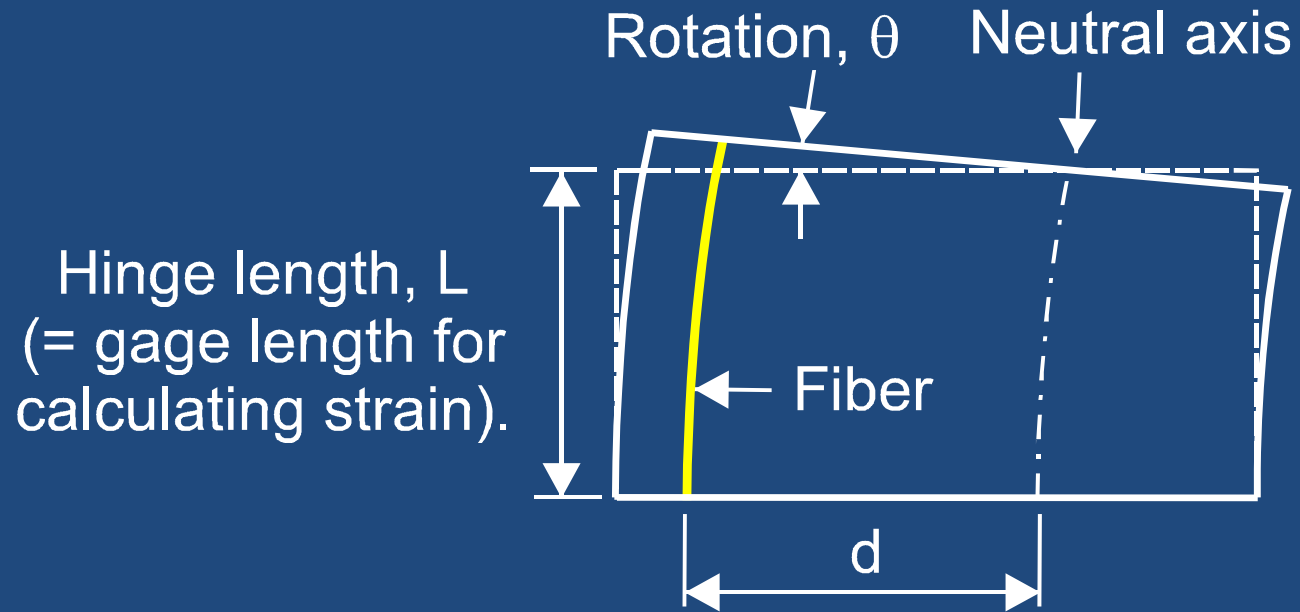
The cross section is represented by a number of uni-axial fibers.
The $M-\psi$ relationship follows from the fiber properties, areas and locations.
Stress-strain relationships reflect the effects of confinement



WALL FIBER MODEL



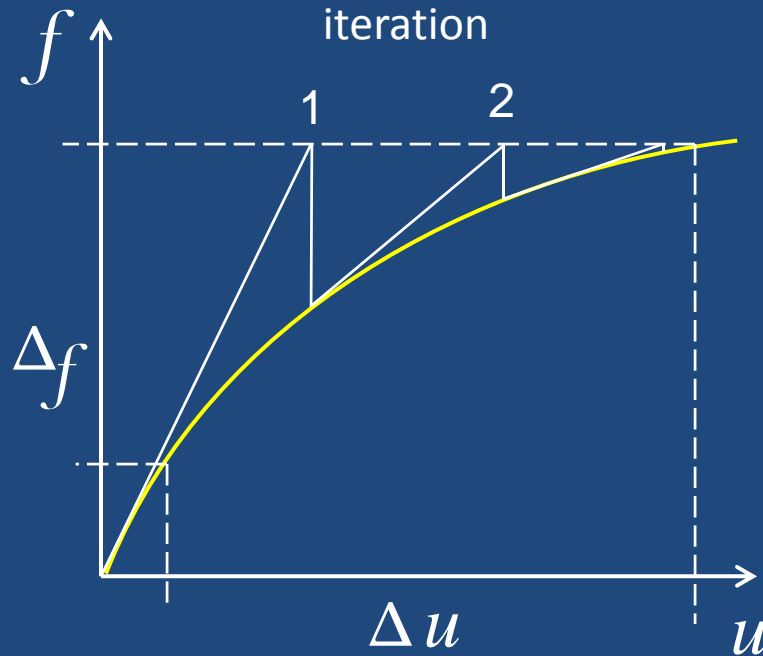
ALTERNATIVE MEASURE - STRAIN



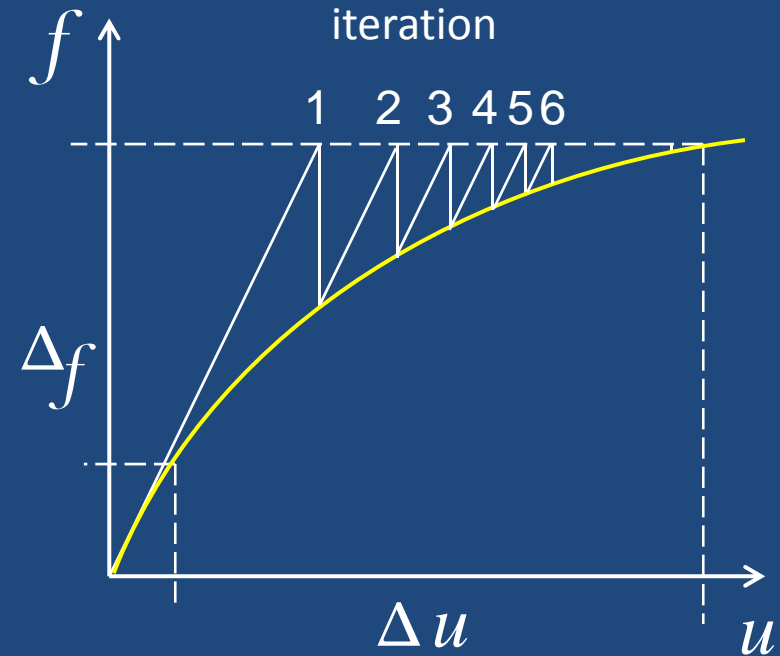
$$\text{Fiber strain} = \frac{\theta d}{L}$$



NONLINEAR SOLUTION SCHEMES



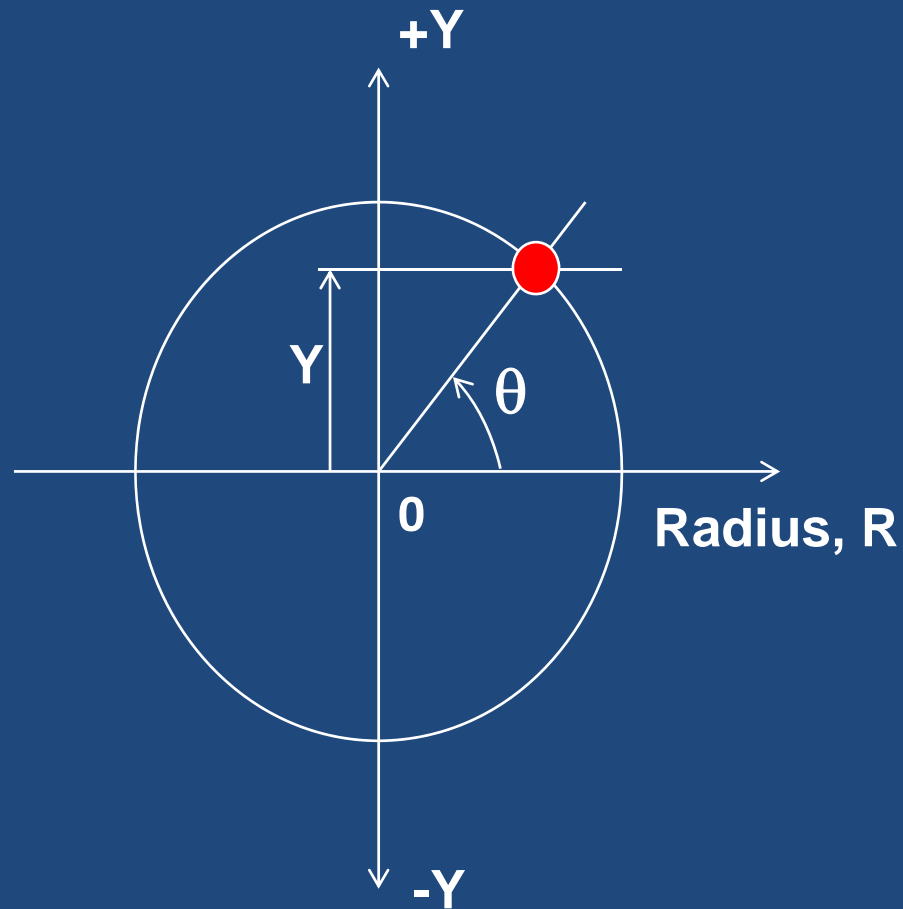
NEWTON – RAPHSON
ITERATION



CONSTANT STIFFNESS
ITERATION

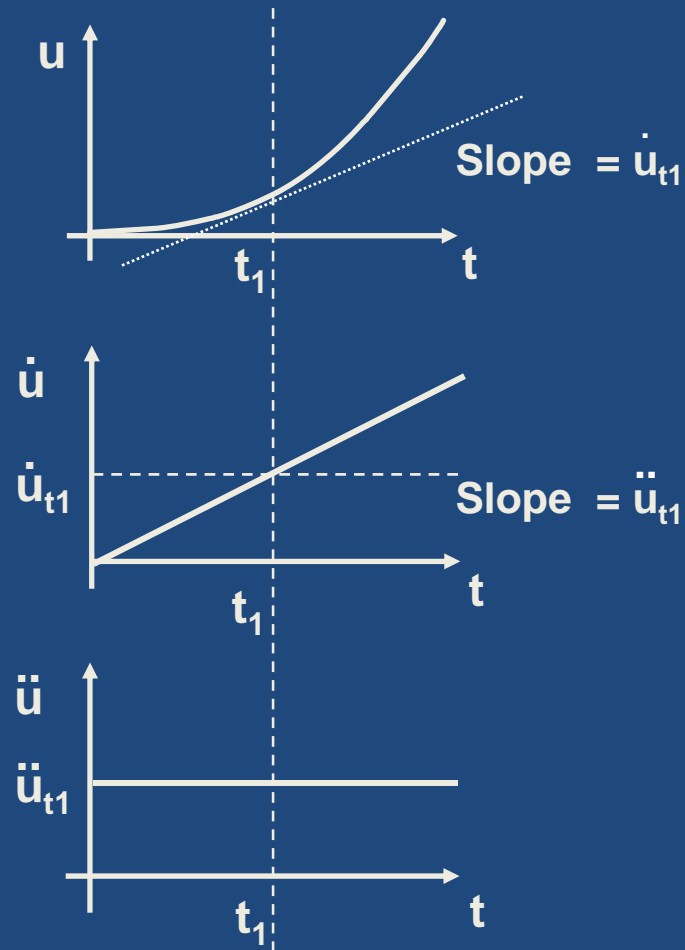


CIRCULAR FREQUENCY





THE D, V & A RELATIONSHIP



UNDAMPED FREE VIBRATION

$$m\ddot{u} + ku = 0$$

$$u_t = u_0 \cos(\omega t)$$

$$\text{where } \omega = \sqrt{\frac{k}{m}}$$



RESPONSE MAXIMA

$$u_t = u_0 \cos(\omega t)$$

$$\dot{u}_t = -\omega u_0 \sin(\omega t)$$

$$\ddot{u}_t = -\omega^2 u_0 \cos(\omega t)$$

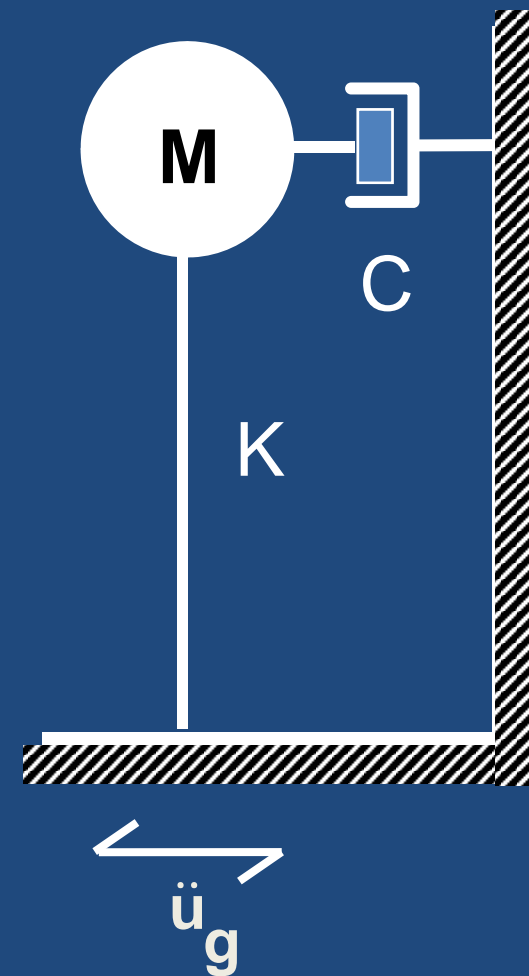
$$\ddot{u}_{\max} = -\omega^2 u_{\max}$$

BASIC DYNAMICS WITH DAMPING

$$M\ddot{u}_t + C\dot{u} + Ku = 0$$

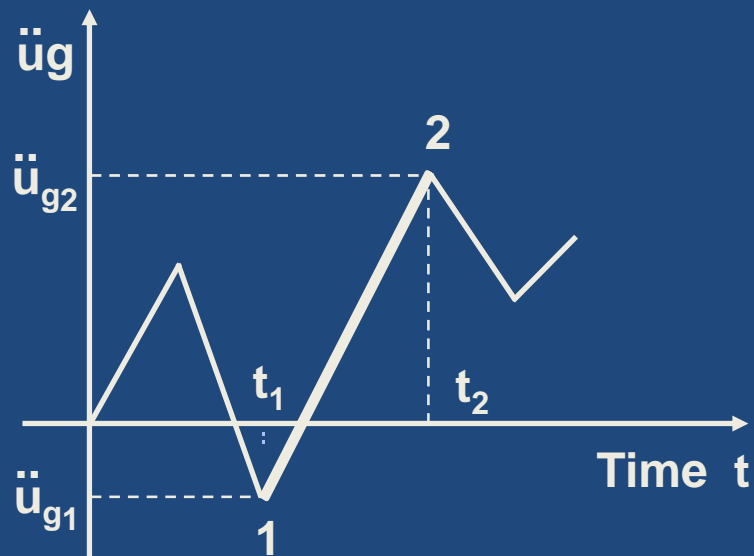
$$M\ddot{u} + C\dot{u} + Ku = -M\ddot{u}_g$$

$$\ddot{u} + 2\xi\omega\dot{u} + \omega^2u = -\ddot{u}_g$$



RESPONSE FROM GROUND MOTION

$$\ddot{u} + 2\xi\omega\dot{u} + \omega^2u = A + Bt = -\ddot{u}_g$$

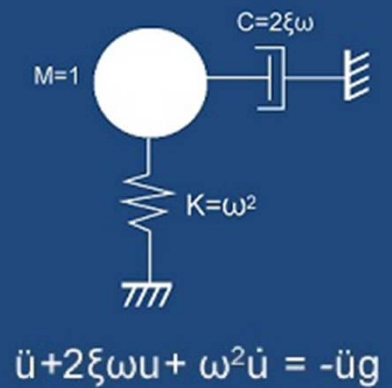
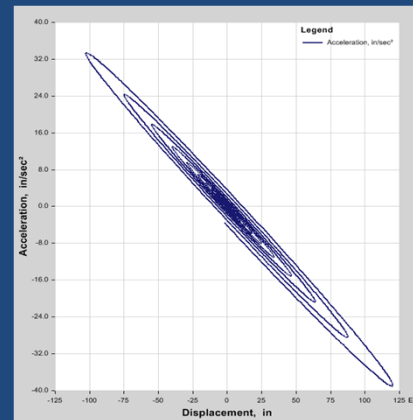
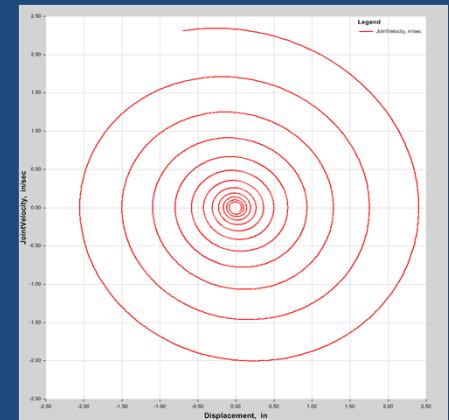
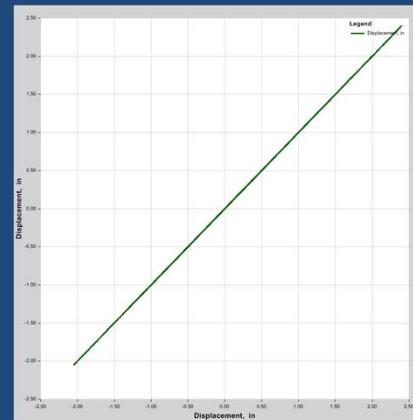
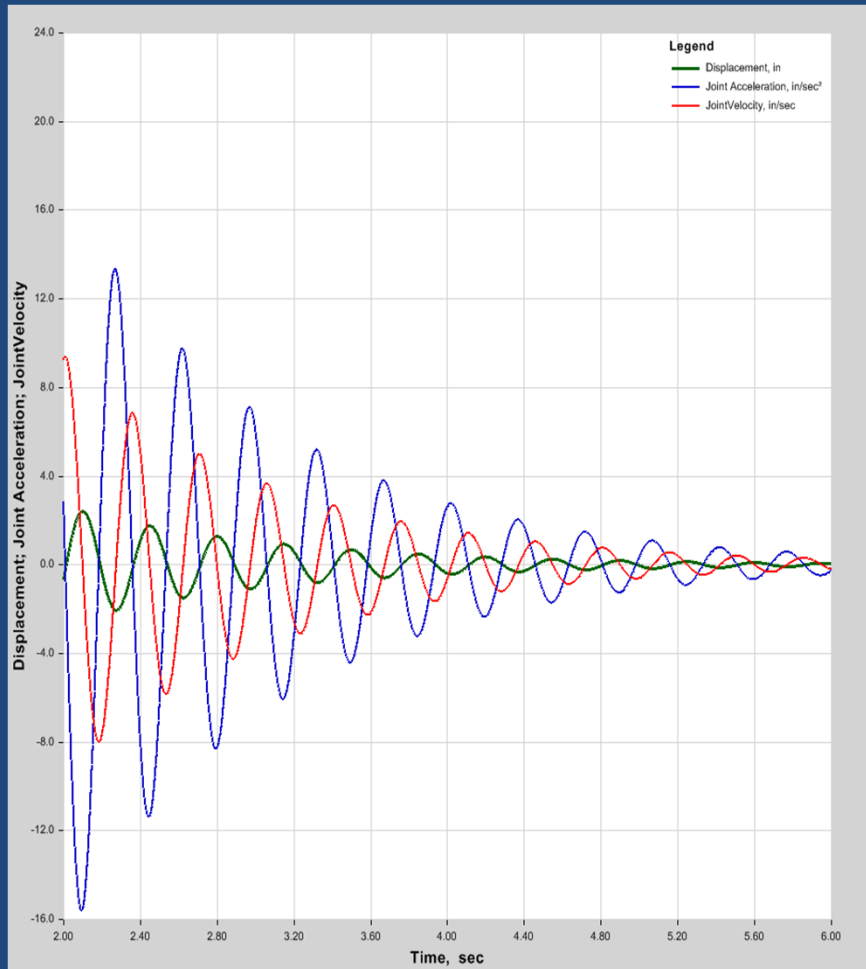


DAMPED RESPONSE

$$\dot{u}_t = e^{-\xi\omega t} \left\{ \left[\dot{u}_{t_1} - \frac{B}{\omega^2} \right] \cos \omega_d t + \frac{1}{\omega_d} \left[A - \omega^2 u_{t_1} - \xi\omega \left(\dot{u}_{t_1} + \frac{B}{\omega^2} \right) \right] \sin \omega_d t \right\} + \frac{B}{\omega^2}$$

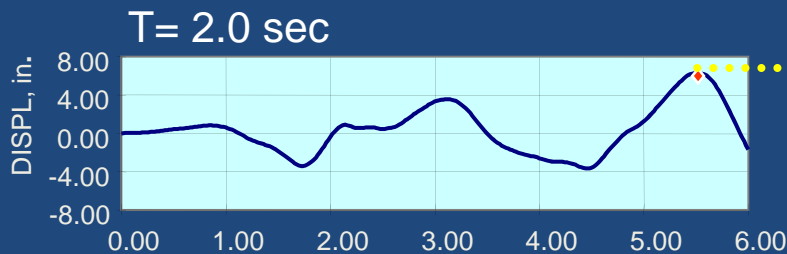
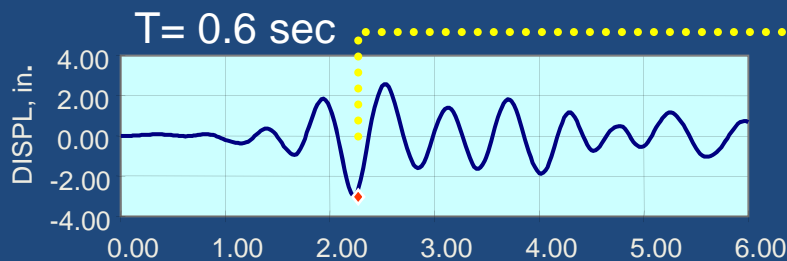
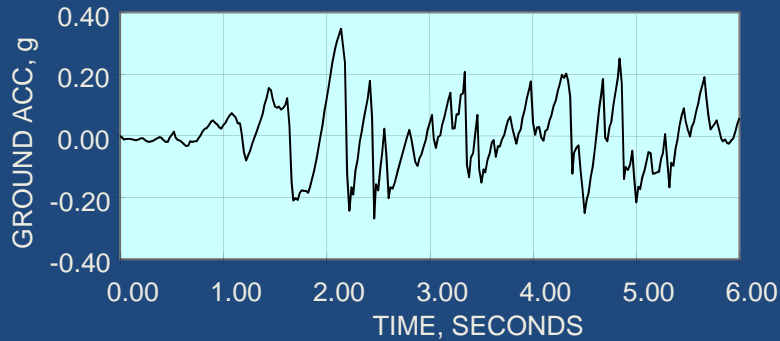
$$u_t = e^{-\xi\omega t} \left\{ \left[u_{t_1} - \frac{A}{\omega^2} + \frac{2\xi B}{\omega^3} \right] \cos \omega_d t + \frac{1}{\omega_d} \left[\dot{u}_{t_1} + \xi\omega u_{t_1} - \frac{\xi A}{\omega} + \frac{B(2\xi^2 - 1)}{\omega^2} \right] \sin \omega_d t \right\} + \left[\frac{A}{\omega^2} - \frac{2\xi B}{\omega^3} + \frac{Bt}{\omega^2} \right]$$

SDOF DAMPED RESPONSE



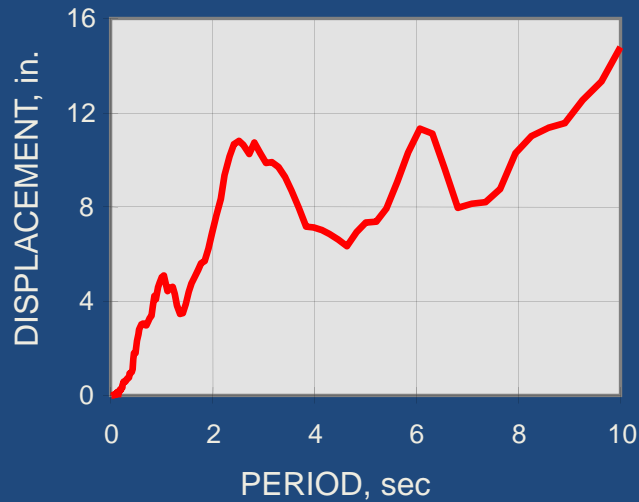
RESPONSE SPECTRUM GENERATION

Earthquake Record



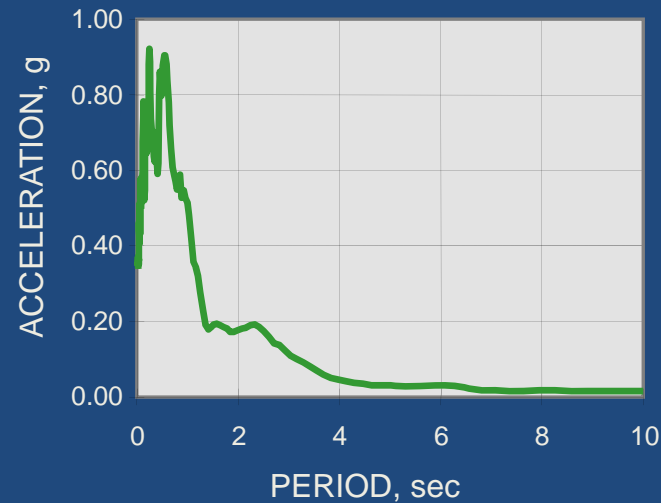
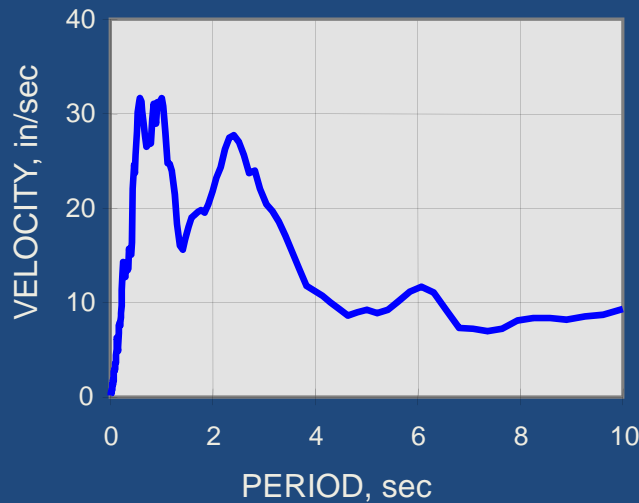
Displacement
Response Spectrum
5% damping

SPECTRAL PARAMETERS



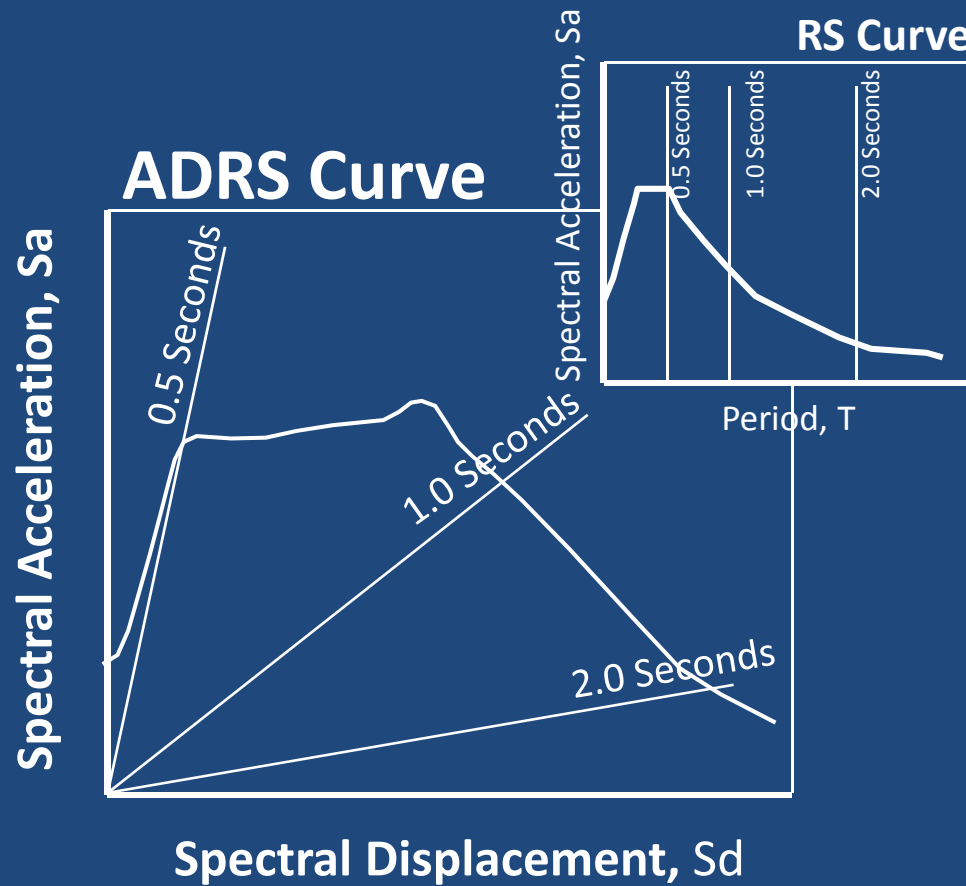
$$PS_v = \omega S_d$$

$$PS_a = \omega PS_v$$



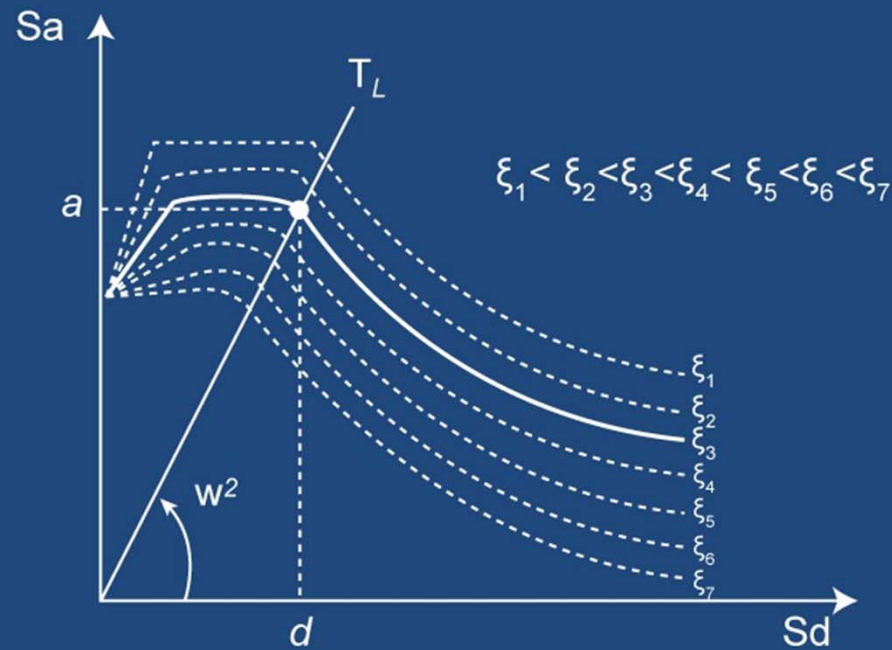


THE ADRS SPECTRUM

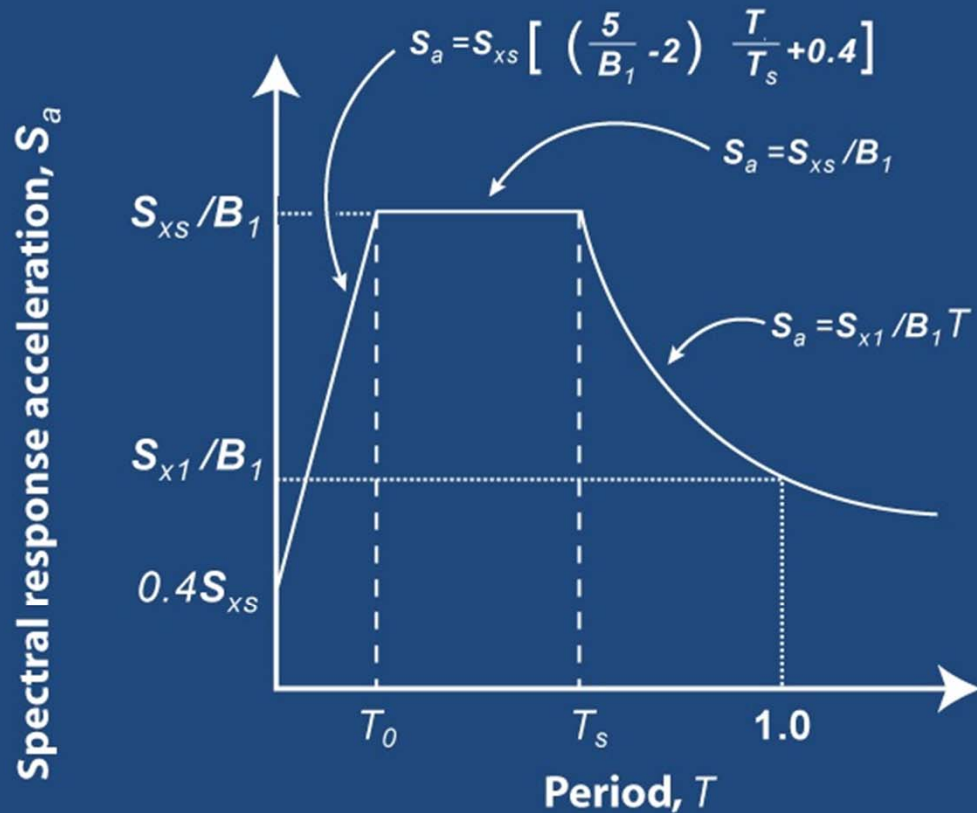




THE ADRS SPECTRUM



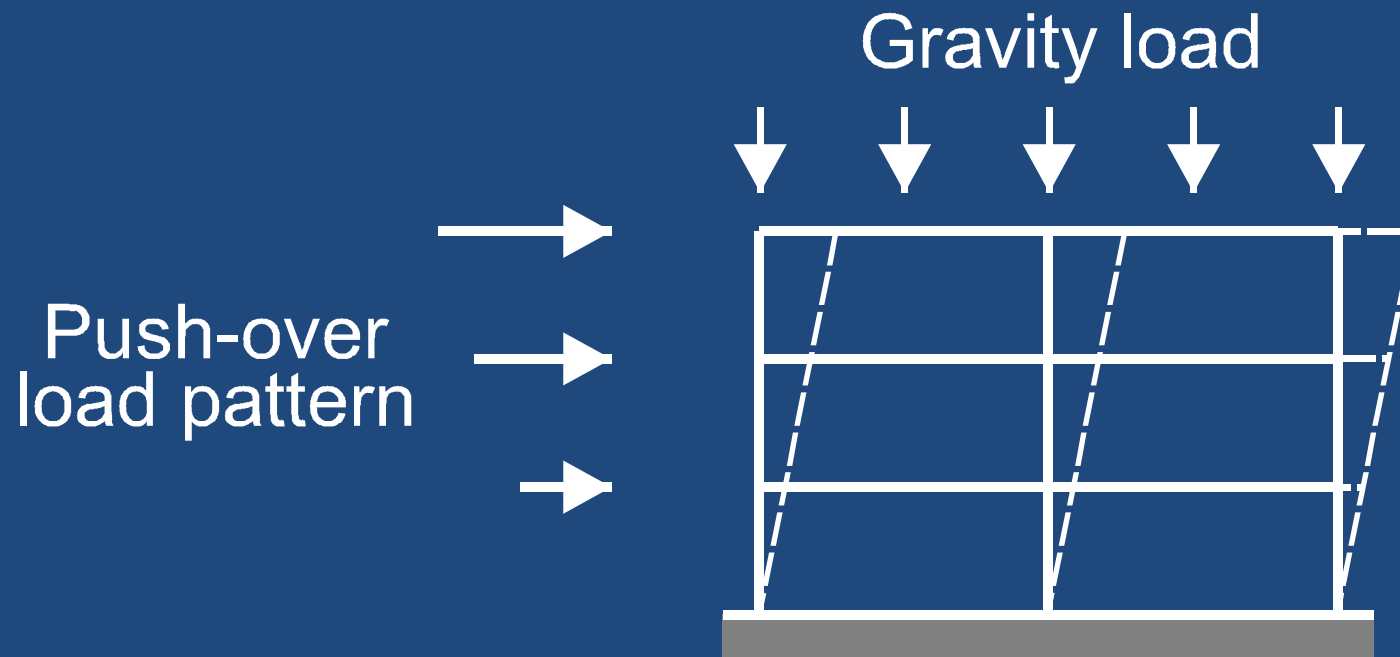
ASCE 7 RESPONSE SPECTRUM



$$B_1 = \frac{4}{5.6 - \log_n(100\xi)}$$

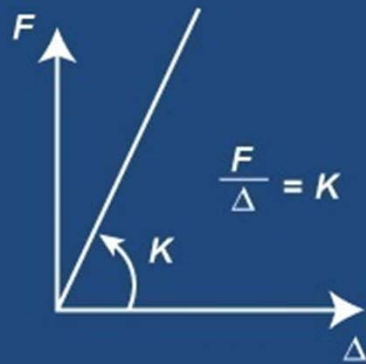


PUSHOVER

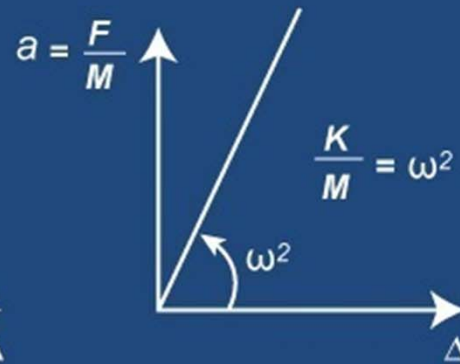




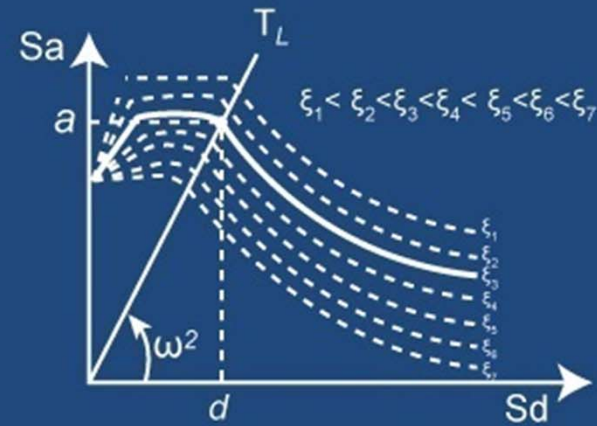
THE LINEAR PUSHOVER



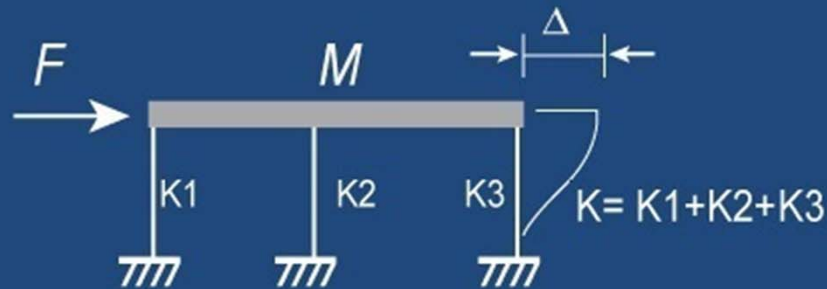
Linear Pushover Diagram
(In terms of force)



Linear Pushover Diagram
(In terms of acceleration)

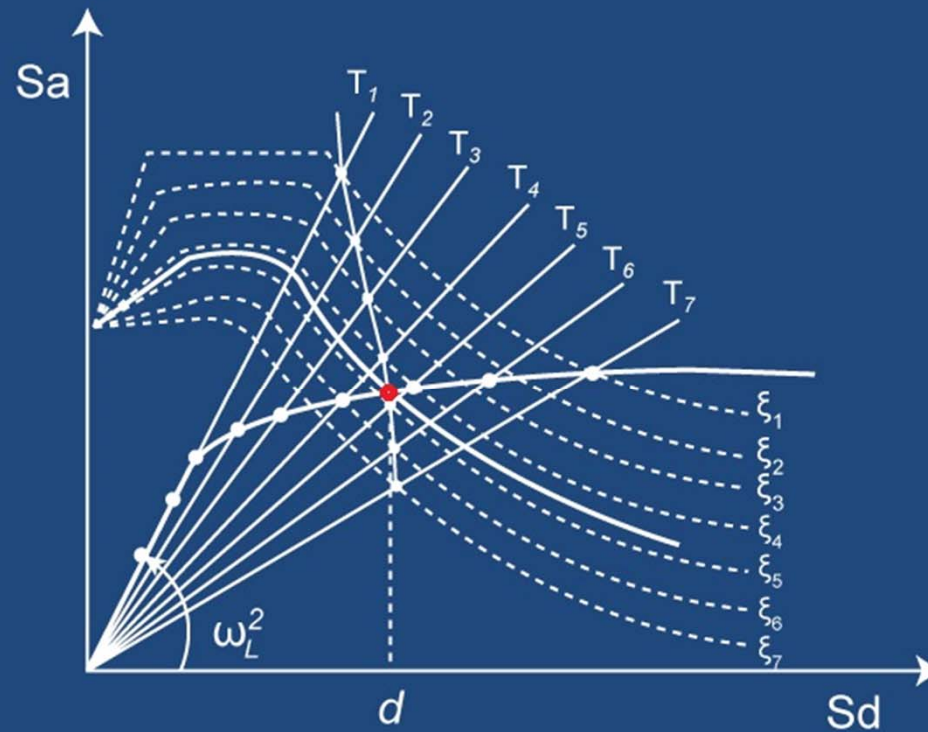


ADRS Spectrum
(With linear pushover diagram)



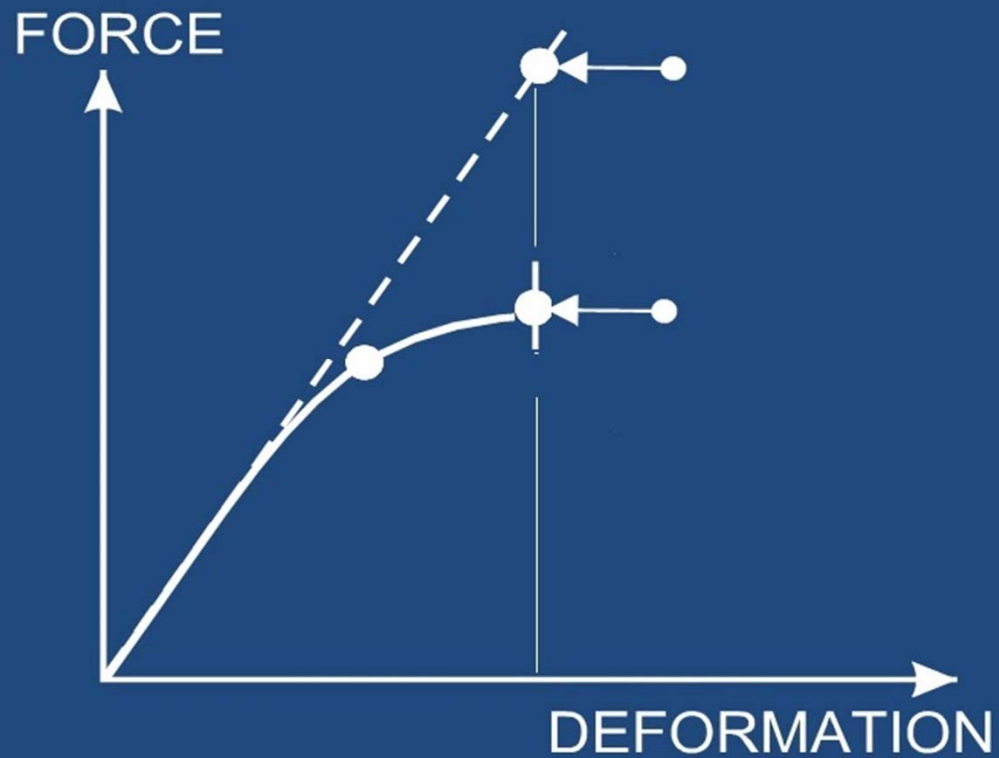
EQUIVALENT LINEARIZATION

How far to push? The Target Point!





DISPLACEMENT MODIFICATION



DISPLACEMENT MODIFICATION

Calculating the Target Displacement

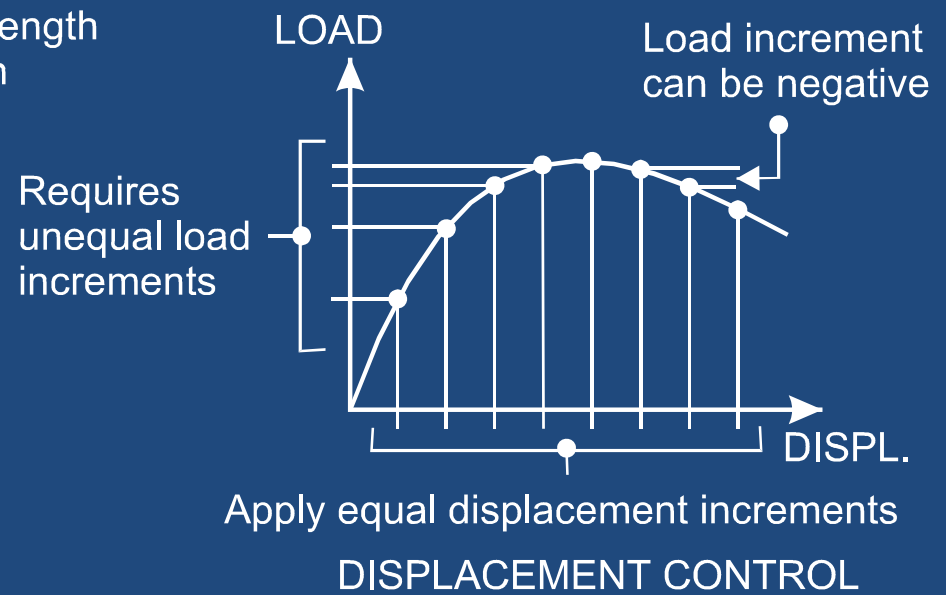
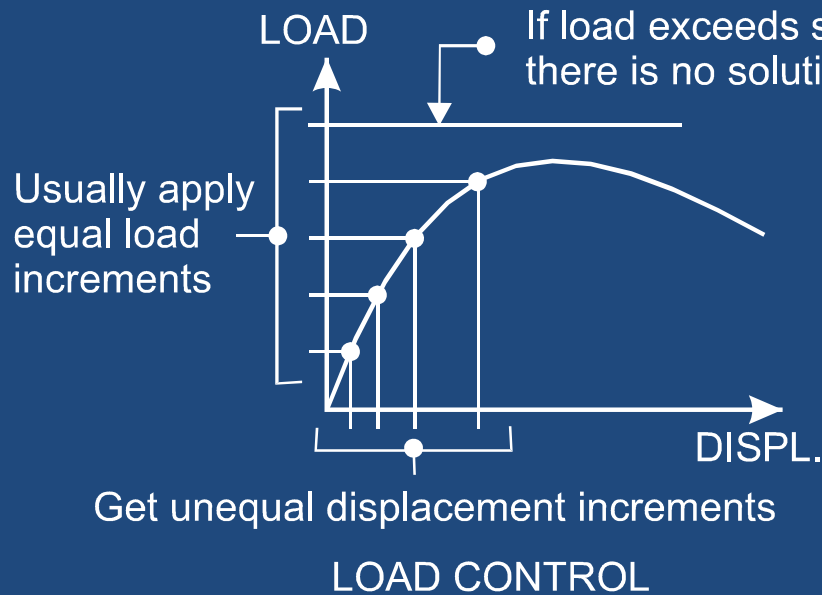
$$\delta = C_0 C_1 C_2 S_a T_e^2 / (4\pi^2)$$

C_0 Relates spectral to roof displacement

C_1 Modifier for inelastic displacement

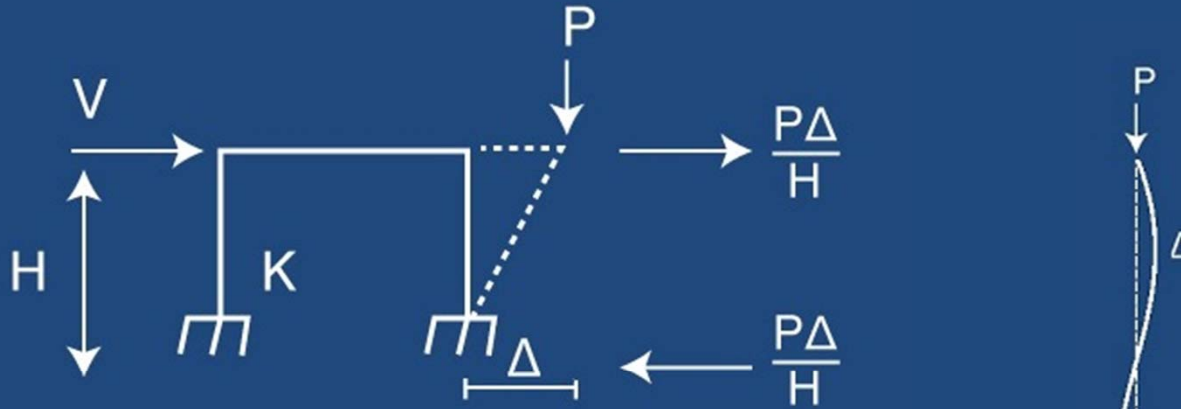
C_2 Modifier for hysteresis loop shape

LOAD CONTROL AND DISPLACEMENT CONTROL





P-DELTA ANALYSIS



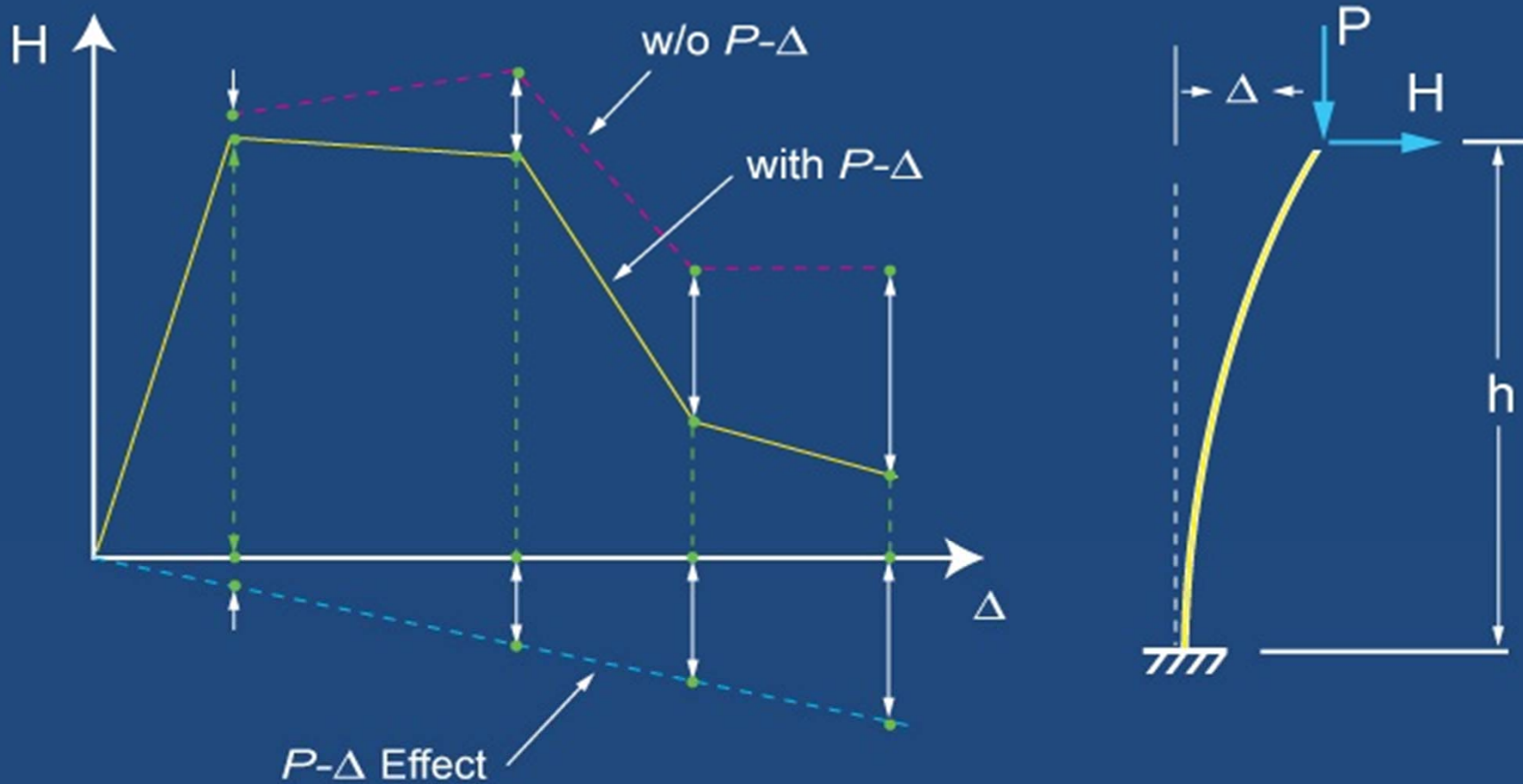
$$V = K\Delta$$

$$V + \frac{P\Delta}{H} = K\Delta$$

$$V = \left(K - \frac{P}{H}\right) \Delta$$

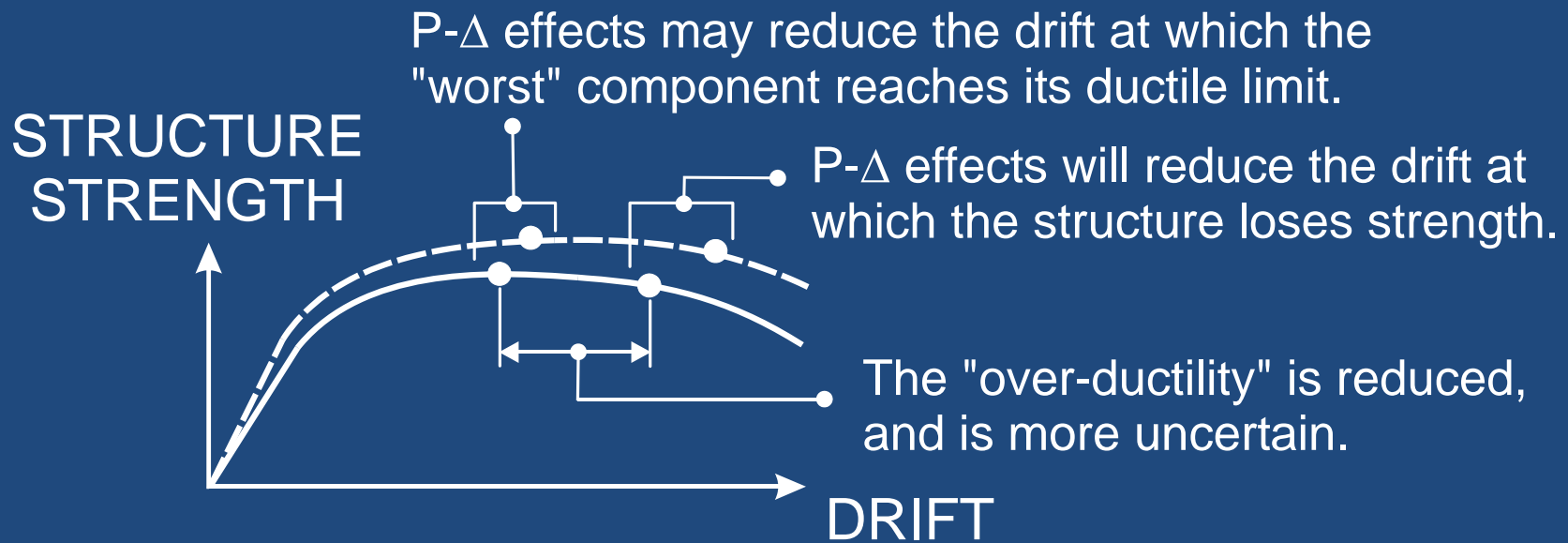


P-DELTA DEGRADES STRENGTH





P-DELTA EFFECTS ON F-D CURVES



THE FAST NONLINEAR ANALYSIS METHOD (FNA)

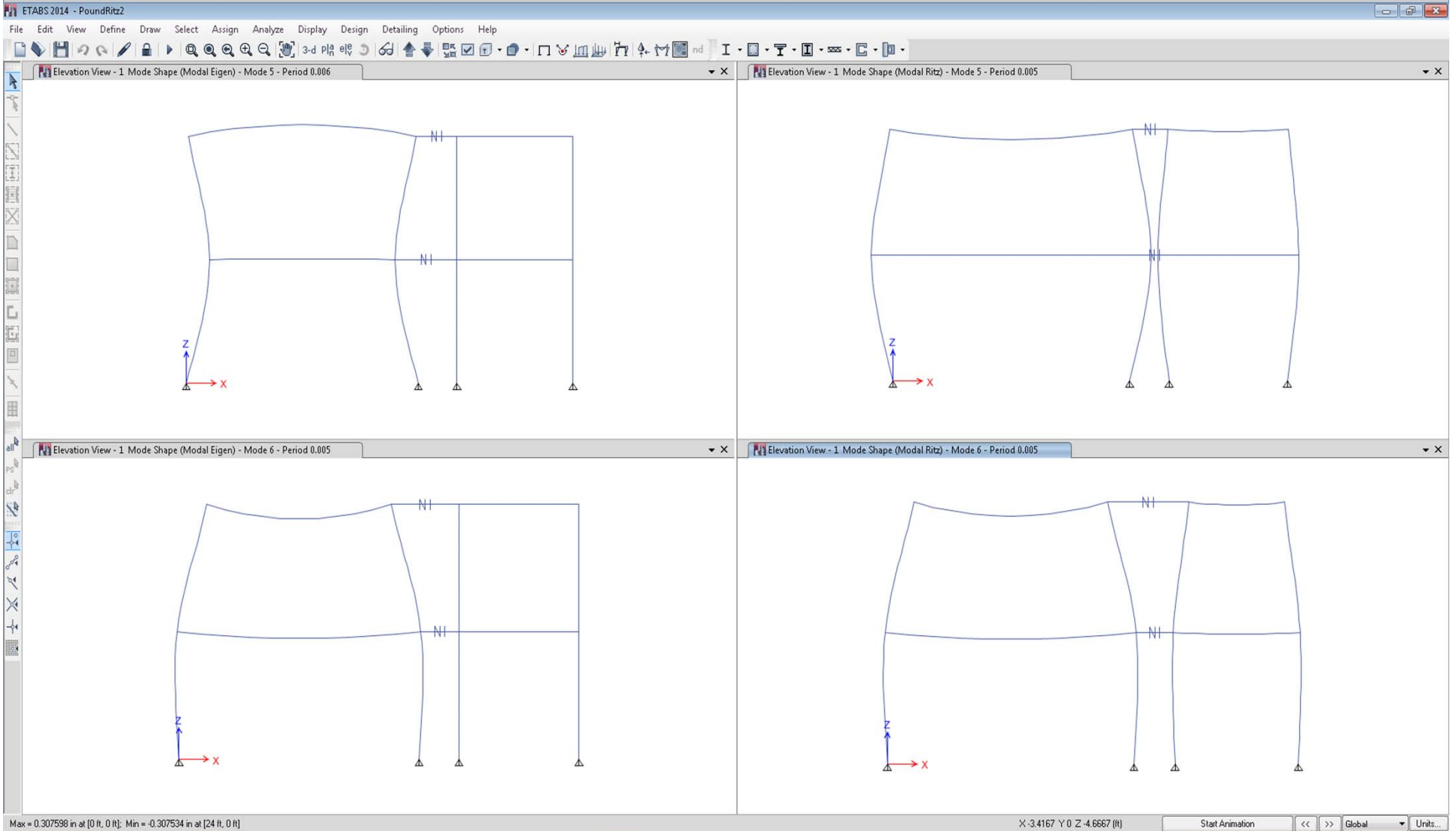
**NON LINEAR FRAME AND SHEAR WALL HINGES
BASE ISOLATORS (RUBBER & FRICTION)**

**STRUCTURAL DAMPERS
STRUCTURAL UPLIFT**

**STRUCTURAL POUNDING
BUCKLING RESTRAINED BRACES**



RITZ VECTORS



FNA KEY POINT

The Ritz modes generated by the nonlinear deformation loads are used to modify the basic structural modes whenever the nonlinear elements go nonlinear.



ARTIFICIAL EARTHQUAKES

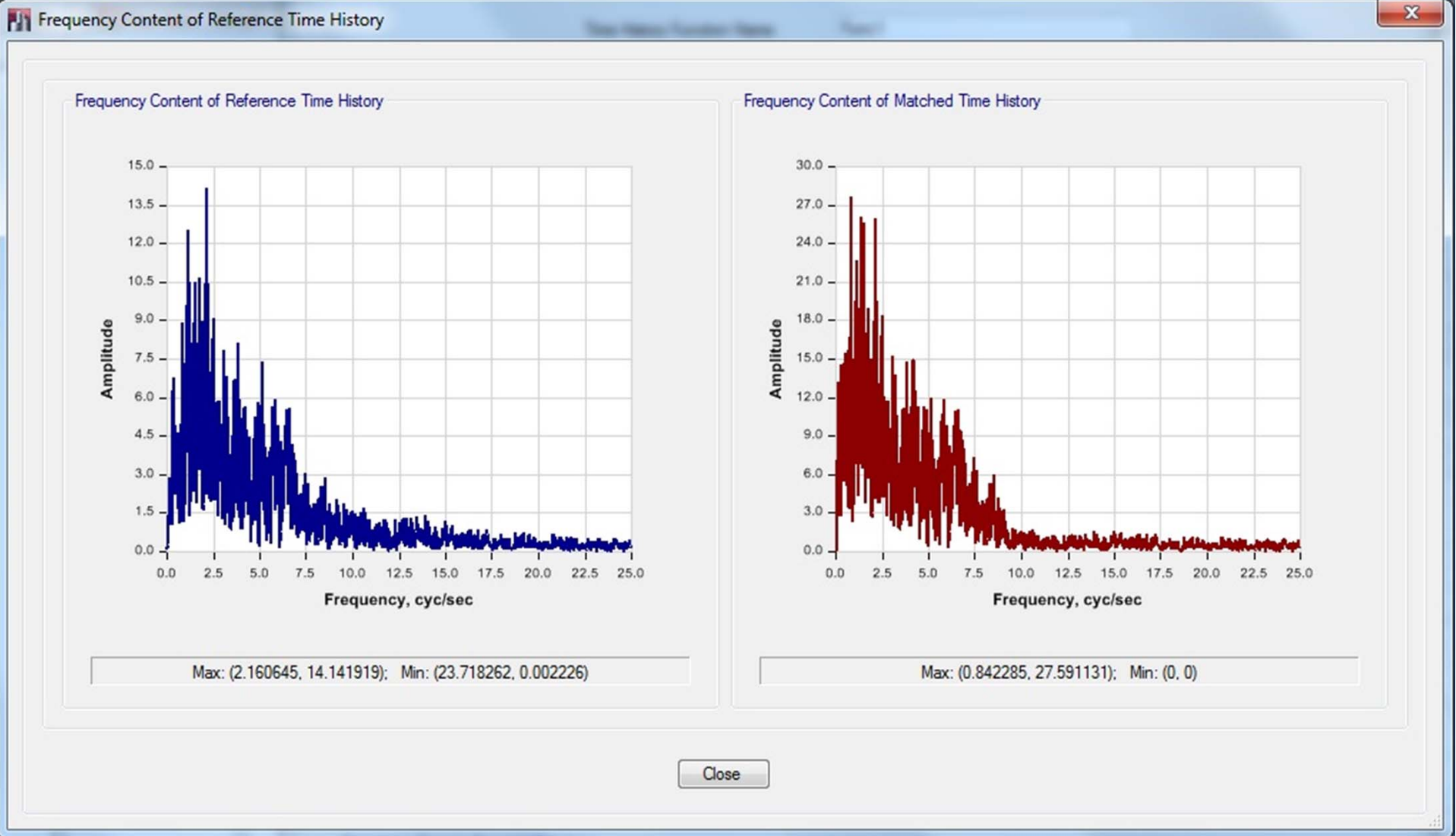
CREATING HISTORIES TO MATCH A SPECTRUM

FREQUENCY CONTENTS OF EARTHQUAKES

FOURIER TRANSFORMS

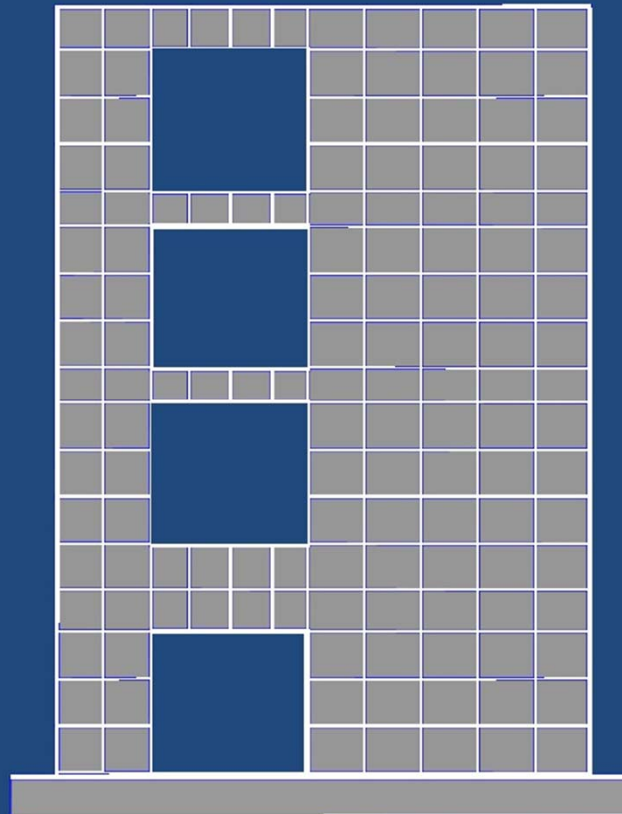


ARTIFICIAL EARTHQUAKES

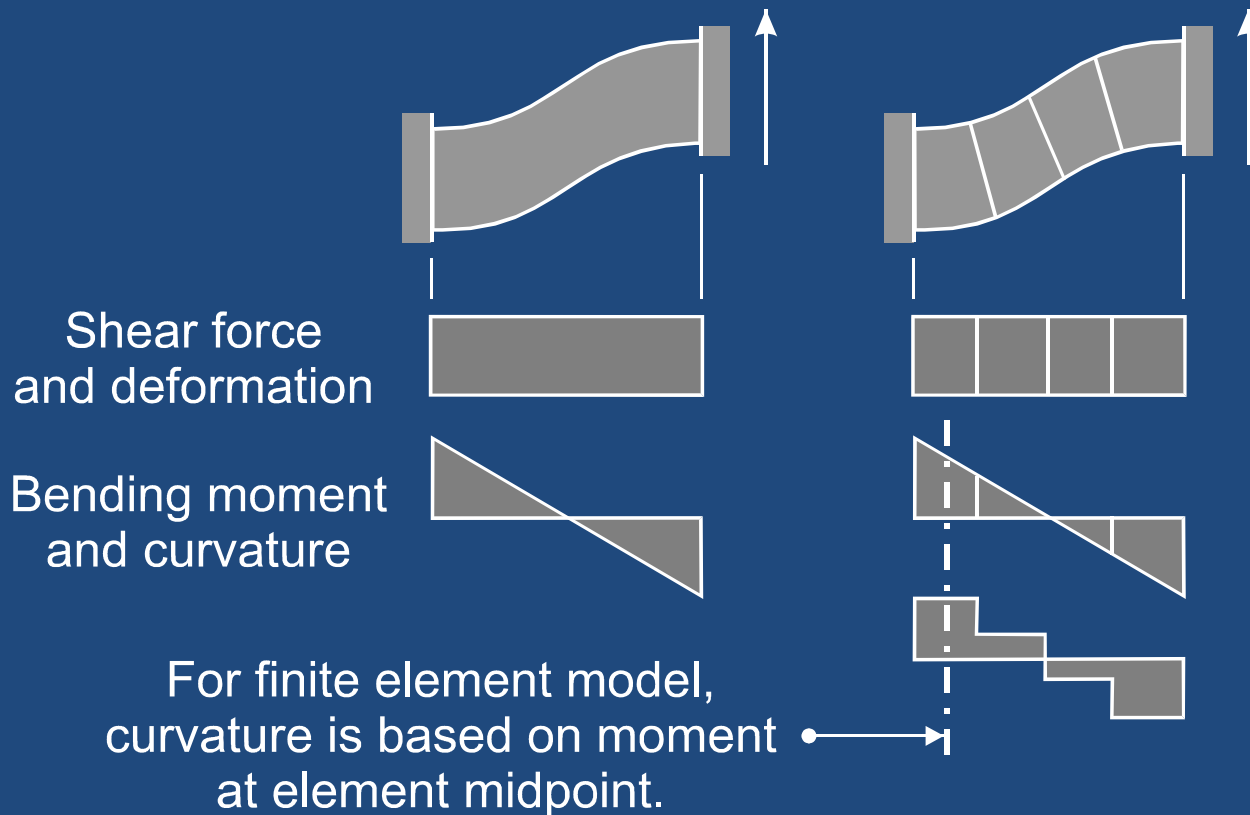




MESH REFINEMENT

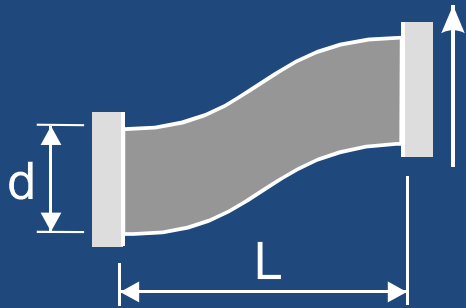


APPROXIMATING BENDING BEHAVIOR



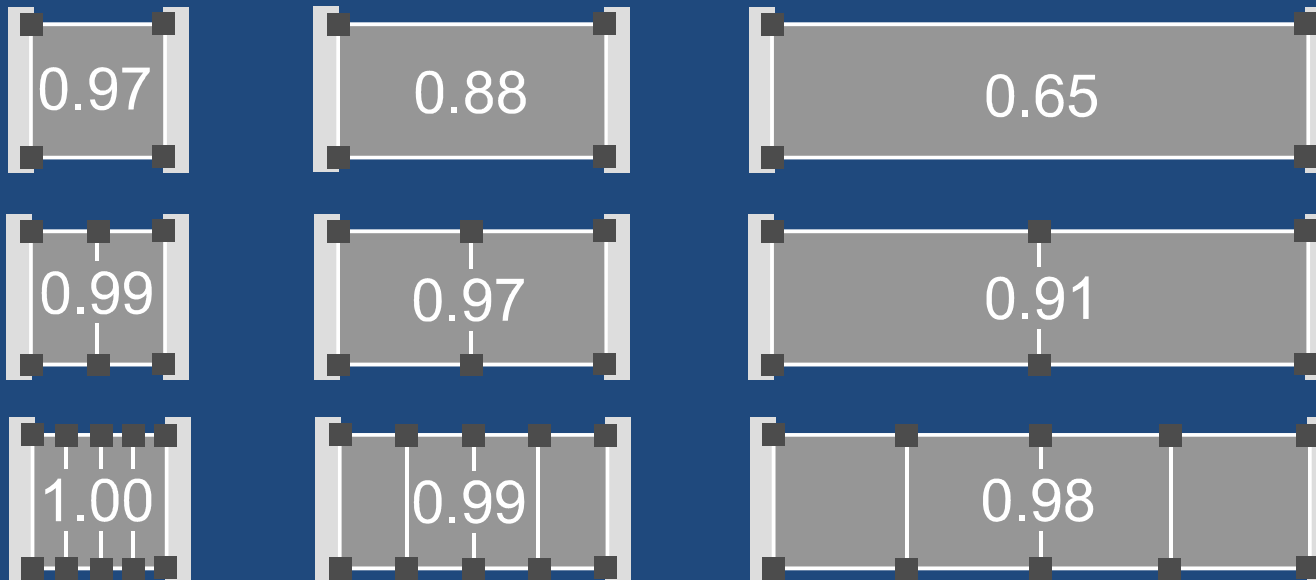
This is for a coupling beam. A slender pier is similar.

ACCURACY OF MESH REFINEMENT



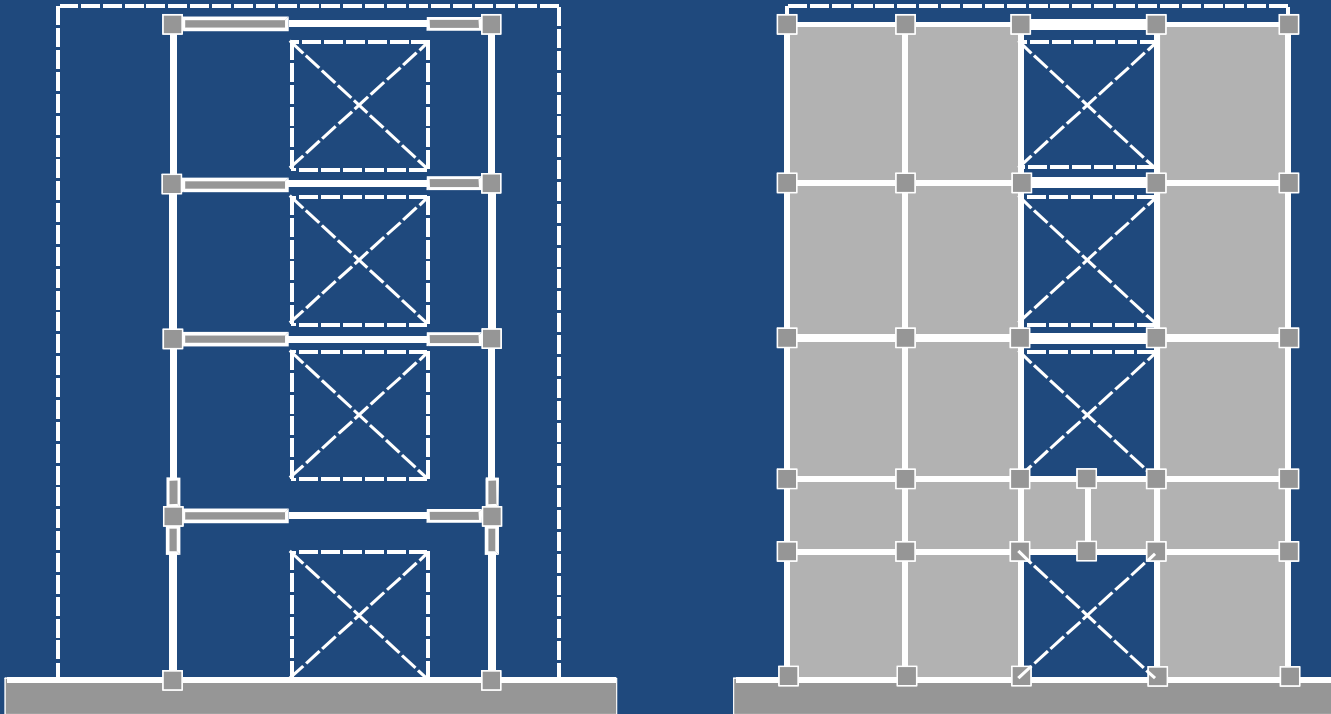
Elastic beam, rectangular section.
 Shear modulus, $G = 0.4E$.
 Assume shear area = actual area.

Ratio of finite element deflection
 to exact deflection for different
 d/L ratios and numbers of elements.

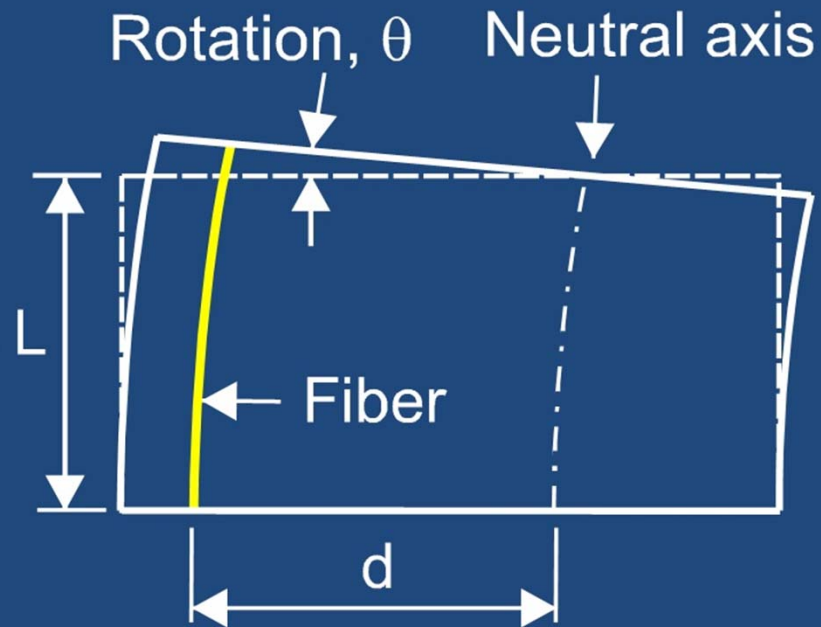




PIER / SPANDREL MODELS



STRAIN & ROTATION MEASURES

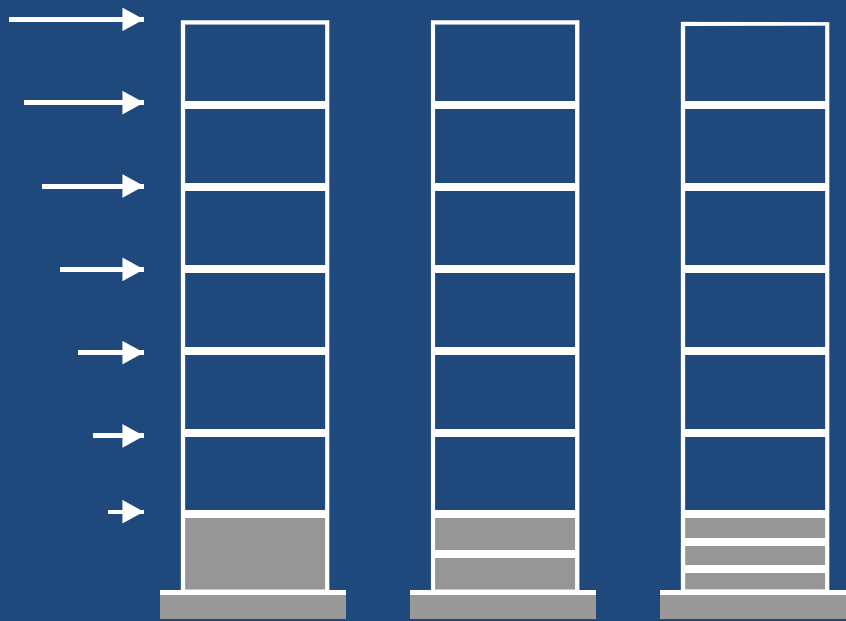


$$\text{Fiber strain} = \frac{\theta d}{L}$$

STRAIN CONCENTRATION STUDY

Gravity load, followed by :

- (1) push-over load with linear variation over height,
- (2) dynamic earthquake load.



1 2 3
Number of elements over hinge length

Use hinge length = story height.

Consider different numbers of elements over the hinge length.

Calculate strain at extreme fiber :

- (a) In lowest element.
- (b) Over story height, using a strain gage.

Calculate rotation over story height, using a rotation gage.

Compare calculated strains and rotations for the 3 cases.

STRAIN CONCENTRATION STUDY

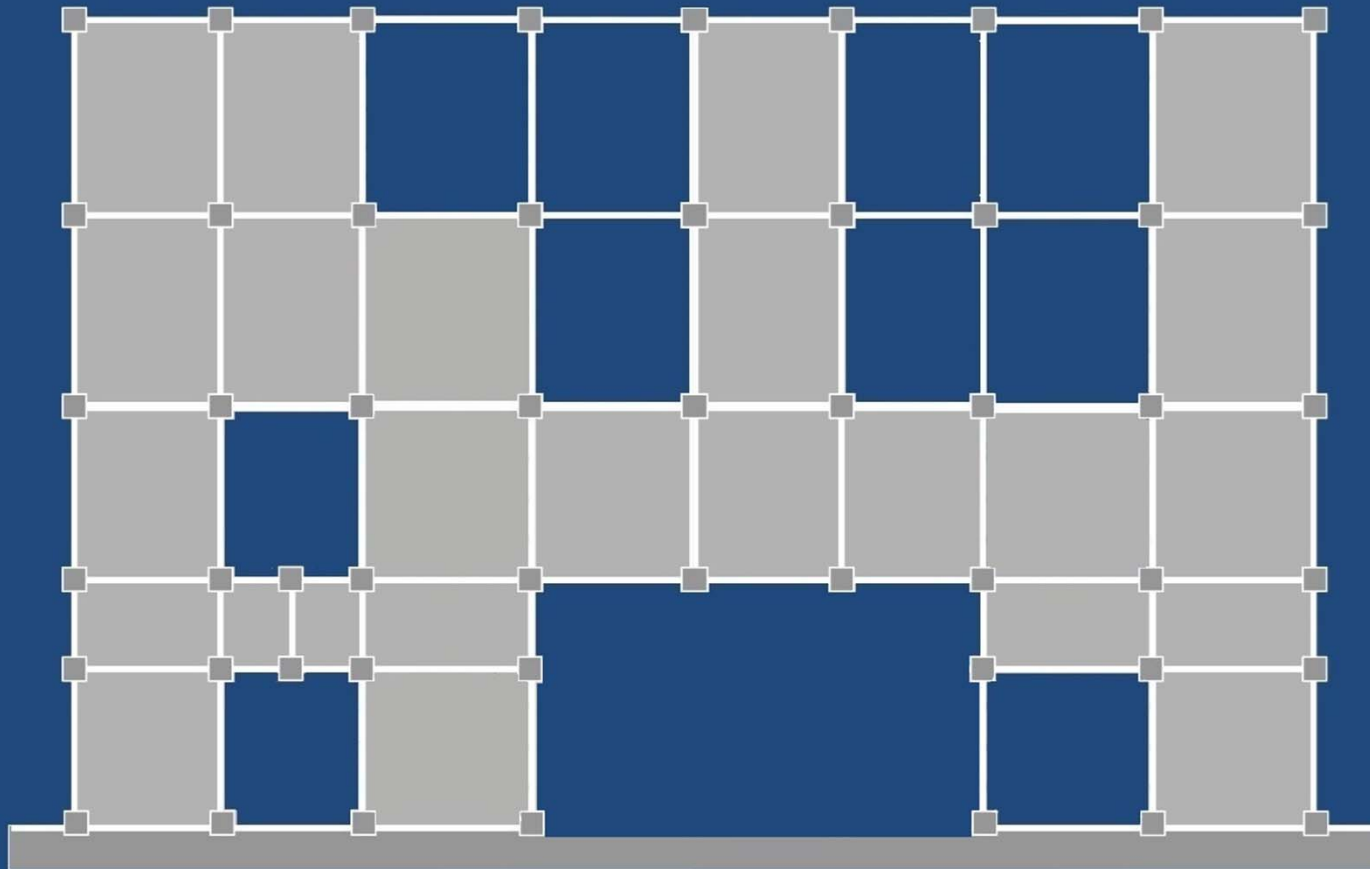
No. of elems	Roof drift	Strain in bottom element	Strain over story height	Rotation over story height
1	2.32%	2.39%	2.39%	1.99%
2	2.32%	3.66%	2.36%	1.97%
3	2.32%	4.17%	2.35%	1.96%

The strain over the story height is insensitive to the number of elements.
Also, the rotation over the story height is insensitive to the number of elements.
Therefore these are good choices for D/C measures.



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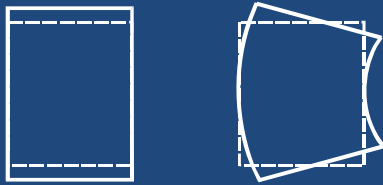
DISCONTINUOUS SHEAR WALLS



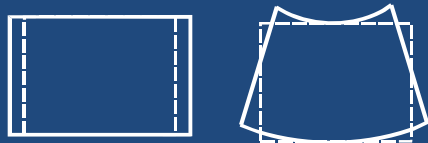
Nonlinear Analysis & Performance Based Design



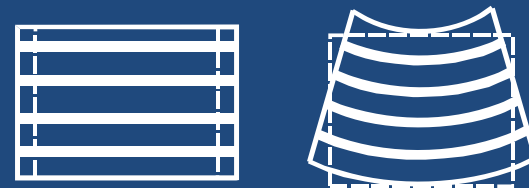
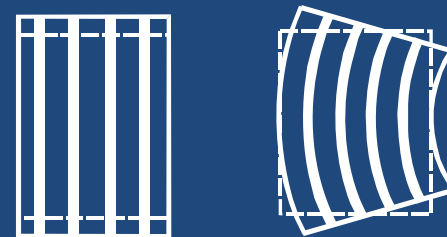
PIER AND SPANDREL FIBER MODELS



Vertical axial and bending

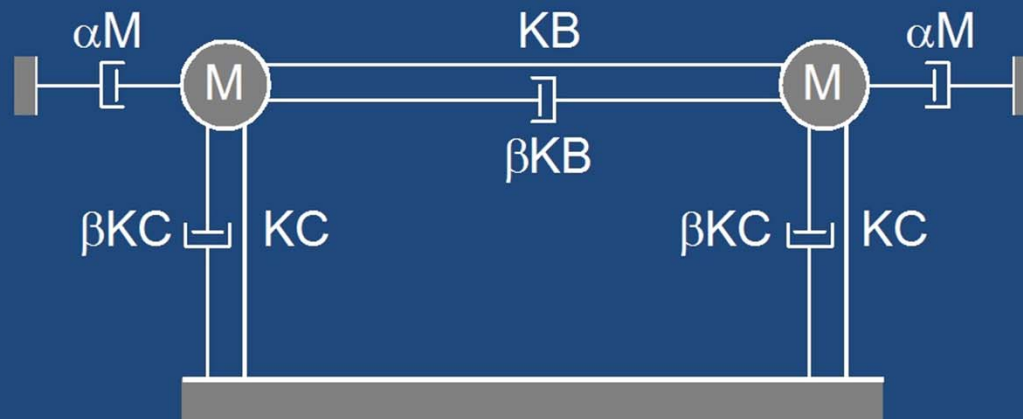


Horizontal axial and bending



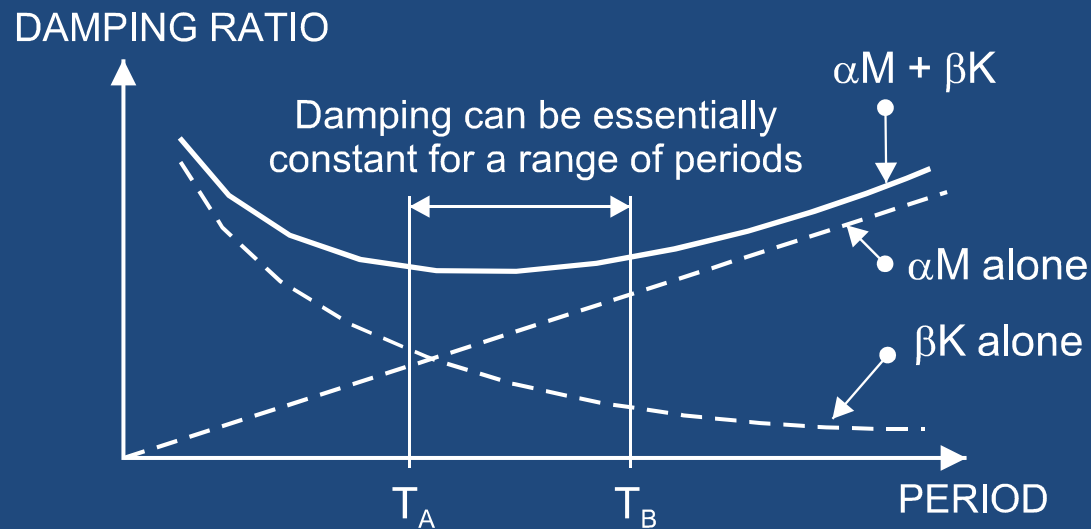
Vertical and horizontal fiber models

RAYLEIGH DAMPING



- The αM dampers connect the masses to the ground. They exert external damping forces. Units of α are $1/T$.
- The βK dampers act in parallel with the elements. They exert internal damping forces. Units of β are T .
- The damping matrix is $\mathbf{C} = \alpha \mathbf{M} + \beta \mathbf{K}$.

RAYLEIGH DAMPING



- For linear analysis, the coefficients α and β can be chosen to give essentially constant damping over a range of mode periods, as shown.
- A possible method is as follows :
 - Choose $T_B = 0.9$ times the first mode period.
 - Choose $T_A = 0.2$ times the first mode period.
 - Calculate α and β to give 5% damping at these two values.
- The damping ratio is essentially constant in the first few modes.
- The damping ratio is higher for the higher modes.

RAYLEIGH DAMPING

$$M\ddot{u}_t + C\dot{u} + Ku = 0$$

$$M\ddot{u}_t + (\alpha M + \beta K)\dot{u} + Ku = 0$$

$$\ddot{u} + \frac{C}{M}\dot{u} + \frac{K}{M}u = 0$$

$$\ddot{u} + 2\xi\omega\dot{u} + \omega^2u = 0 \quad ; \quad 2\xi M\omega = C$$

$$\xi = \frac{C}{2M\omega} = \frac{C}{2M\sqrt{\frac{K}{M}}} = \frac{C}{2\sqrt{KM}} = \frac{\alpha M}{2\sqrt{KM}} + \frac{\beta K}{2\sqrt{KM}}$$

$$\xi = \frac{\alpha}{2\omega} + \frac{\beta\omega}{2}$$

RAYLEIGH DAMPING

Higher Modes (high ω) = β

Lower Modes (low ω) = α

To get ζ from α & β for any $\omega = \sqrt{\frac{K}{M}}$; $T = \frac{2\pi}{\omega}$

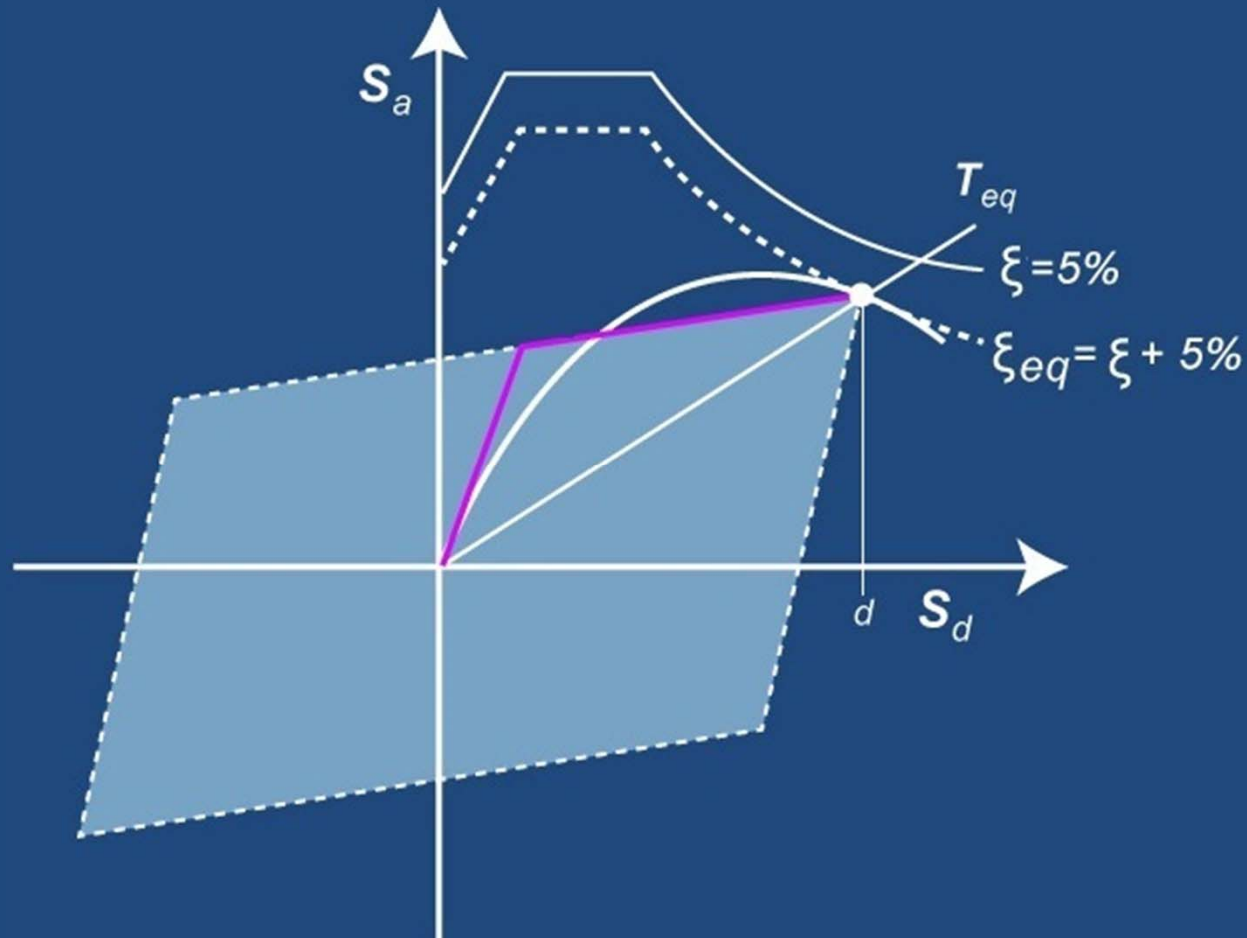
To get α & β from two values of ζ_1 & ζ_2

$$\zeta_1 = \frac{\alpha}{2\omega_1} + \frac{\beta\omega_1}{2}$$

Solve for α & β

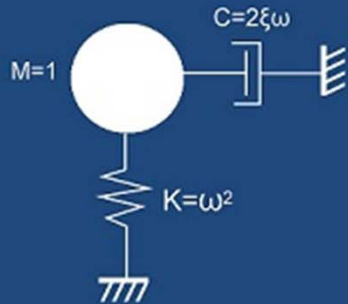
$$\zeta_2 = \frac{\alpha}{2\omega_2} + \frac{\beta\omega_2}{2}$$

DAMPING COEFFICIENT FROM HYSTERESIS





DAMPING COEFFICIENT FROM HYSTERESIS



$$\ddot{u} + 2\xi\omega\dot{u} + \omega^2 u = -\ddot{u}_g$$

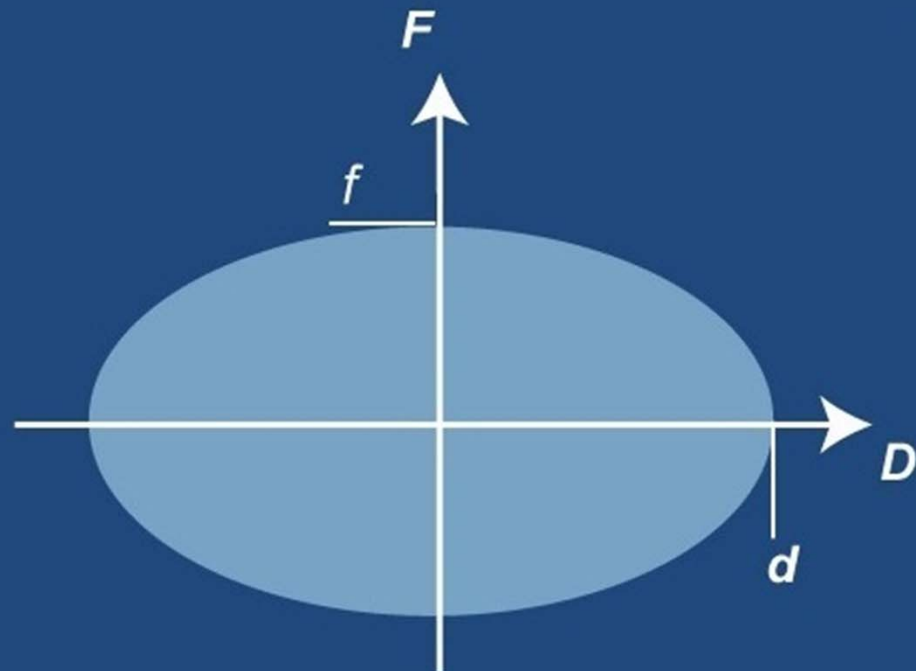
$$u = d \sin \omega t$$

$$\dot{u} = d \omega \cos \omega t$$

$$f = (2\xi\omega) (d\omega)$$

$$\text{Area} = \pi f d$$

$$= 2\pi\xi\omega^2 d^2$$



A BIG THANK YOU!!!

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- American Concrete Institute Board of Directors, Spring 2011

